



DARK ENERGY
SURVEY

Photo-z Requirements for Self-Calibration of Cluster Dark Energy Studies

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Outline

- Cluster mass function
- Number counts and Covariance
- Mass-Observable relation
- Self-Calibration
- Results



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Mass function

- Cluster mass-function **exponentially** sensitive to linear density perturbations σ

$$\frac{d\bar{n}}{d\ln M} = 0.3 \frac{\rho_m}{M} \frac{d\ln \sigma^{-1}}{d\ln M} \exp\left[-|\ln \sigma^{-1} + 0.64|^{3.82}\right]$$

Jenkins et al. 2001

⇒ Cluster number counts sensitive to
DE parameters.



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Number Density

- Number density in bin i (z , M , angle, etc...)

$$\bar{n}_i = \int_{M_i^{obs}}^{M_{i+1}^{obs}} d \ln M^{obs} \int d \ln M \frac{d\bar{n}}{d \ln M} p(M^{obs} | M)$$

where

$$p(M^{obs} | M) = \frac{1}{\sqrt{2\pi\sigma_{\ln M}^2(z)}} \exp \left[- \left(\frac{\ln M^{obs} - \ln M - \ln M^{bias}(z)}{\sqrt{2\sigma_{\ln M}^2(z)}} \right)^2 \right]$$



Number Counts

- Volume element $dV = \frac{D_A^2(z)}{H(z)} dz d\Omega$
- Number counts

$$\bar{N}_i = \Delta\Omega \int_{z_i^{phot}}^{z_{i+1}^{phot}} dz^{phot} \int dz \frac{D_A^2}{H} \bar{n}_i(z) p(z^{phot} | z)$$

where

$$p(z^{phot} | z) = \frac{1}{\sqrt{2\pi\sigma_z^2(z)}} \exp\left[-\left(\frac{z^{phot} - z - z^{bias}(z)}{\sqrt{2\sigma_z^2(z)}}\right)^2\right]$$



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Sample Covariance

$$\begin{aligned} S_{ij} &= \langle (N_i - \bar{N}_i)(N_j - \bar{N}_j) \rangle \\ &= b_i b_j \bar{n}_i \bar{n}_j \int \frac{d^3 k}{(2\pi)^3} W_i^*(\vec{k}) W_j(\vec{k}) P(k) \end{aligned}$$

where the window $W_i(\vec{k})$ is convolved with the **photo-z** distribution.



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Mass-Observable Relation: Redshift Evolution

- **Arbitrary** (2 mass parameters per bin)
- **Mean** relation: **Power law**

$$\frac{M(z_i)}{M_{fid}} = e^A (1 + z_i)^n \left(\frac{O}{O_{fid}} \right)^p$$

Assume p is known.

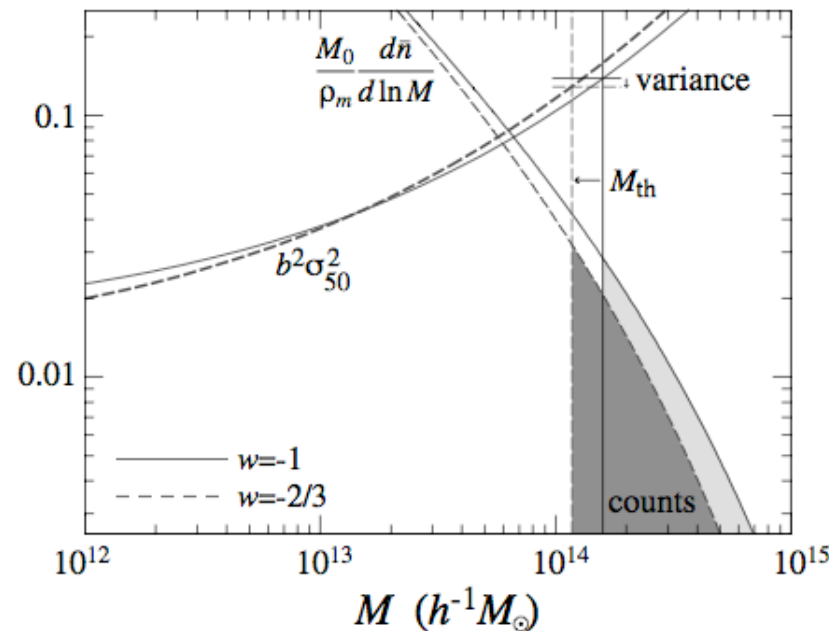
- **Scatter**: Polynomial (**cubic**)

$$\sigma_{\ln M}^2(z_i) = \sigma_{\ln M}^2(z_i) \Big|_{fid} + \sum_{k=0}^3 B_k z_i^k$$



Uncertainties

- **Mass** and **redshift uncertainties** change the observed number counts and are degenerate with DE.





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Self-Calibration

- “Self-calibration” of mass-observable parameters: consistency between number counts and

- 1) clustering

Majumdar & Mohr 2004; Lima & Hu 2004

- 2) shape of observed mass function

Hu 2003; Lima & Hu 2005

- 3) follow up

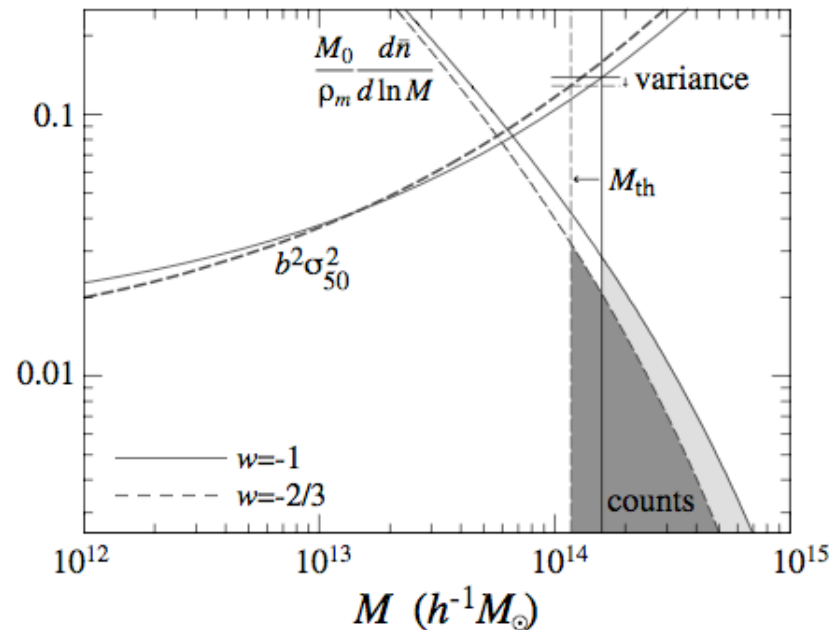
Majumdar & Mohr 2003, 2004



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Self-Calibration

- **Clustering**: Requiring consistency between **counts** and sample **variance** breaks degeneracy between **shifts in mass** and **DE** variations .

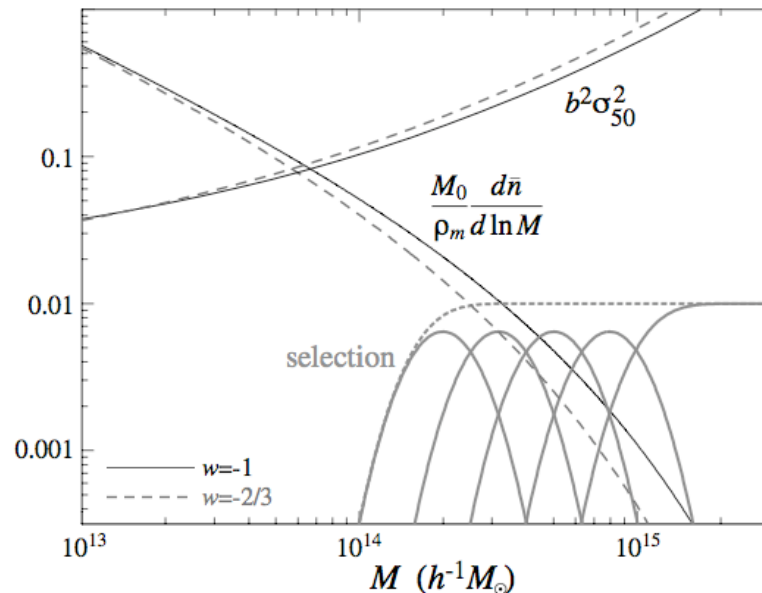




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Self-Calibration

- **Shape**: Measuring number **counts** as a function of **mass** provides **observed** mass function. Consistency breaks degeneracy of DE with **scatter** in mass-observable.



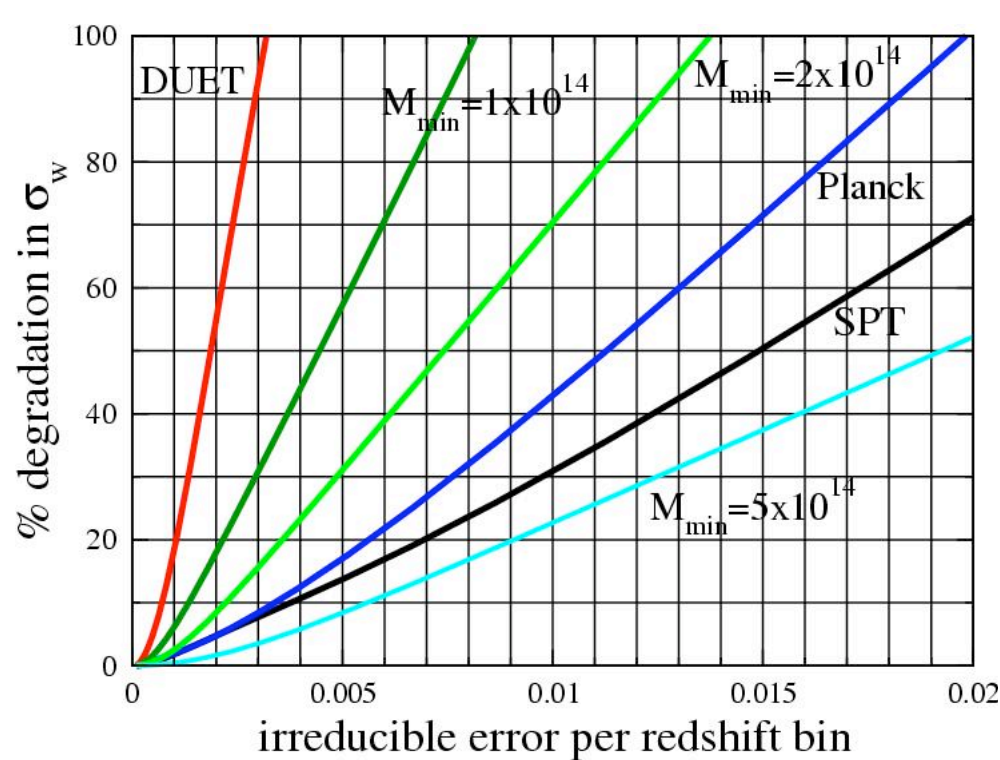
Lima & Hu 2005



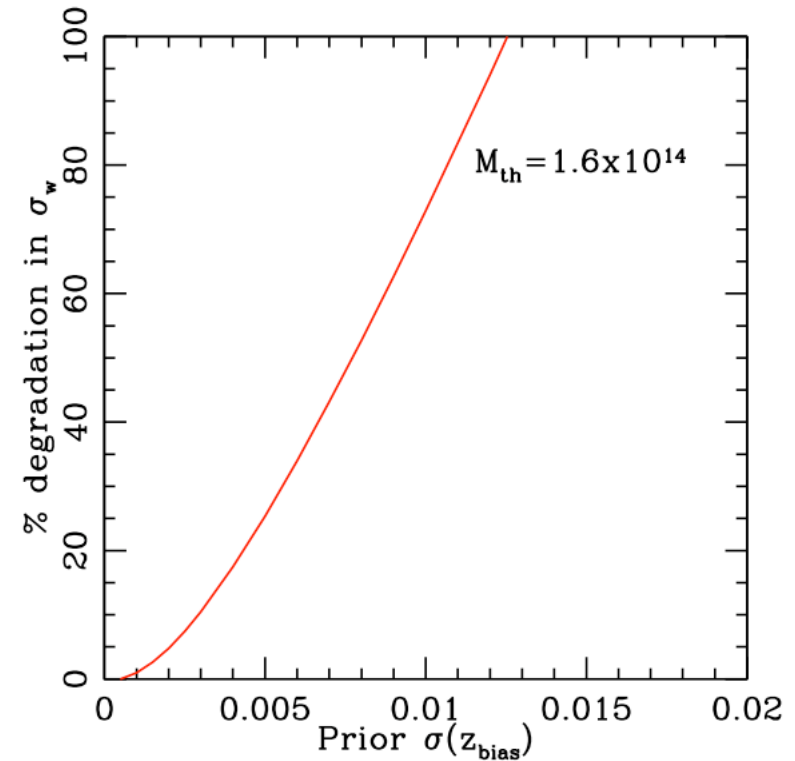
Previous studies

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- Fixed mass-observable. No z scatter. Prioired z bias.
- Counts only



Huterer et al. 2004



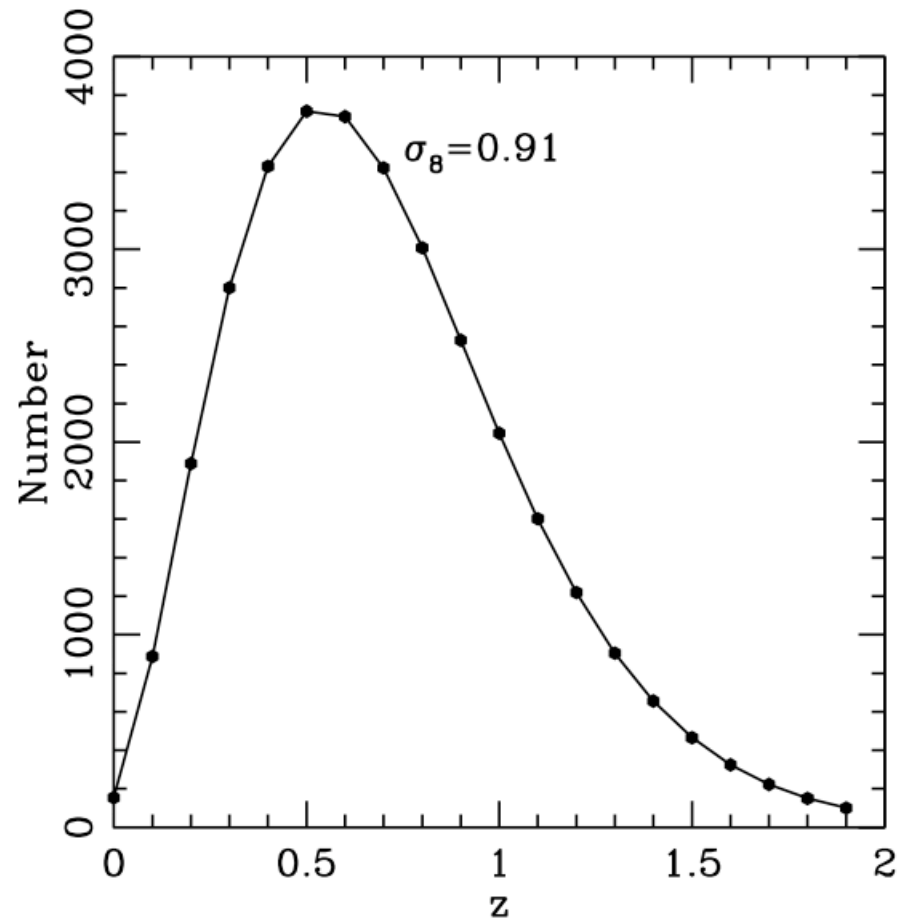


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Number Counts

SPT like
4000 deg²
 $\Delta z = 0.1$ bins

WMAP 1yr





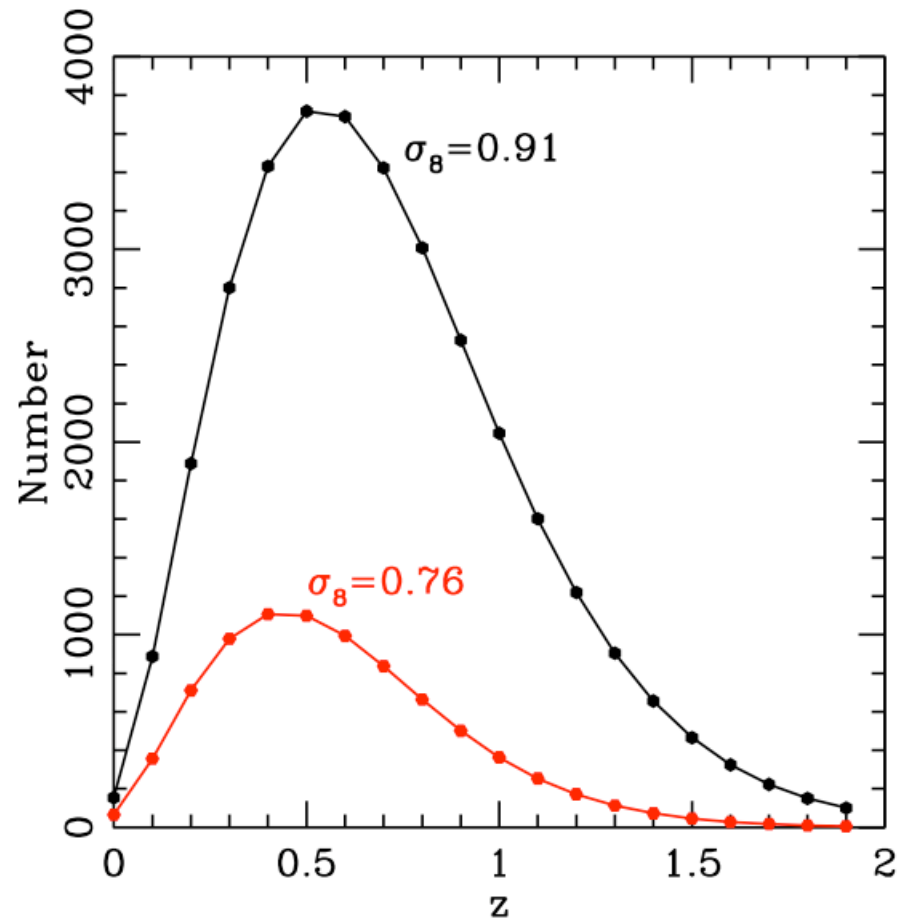
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Number Counts

SPT like
4000 deg²
 $\Delta z = 0.1$ bins

WMAP 1yr

WMAP 3yr
(4 x less!)



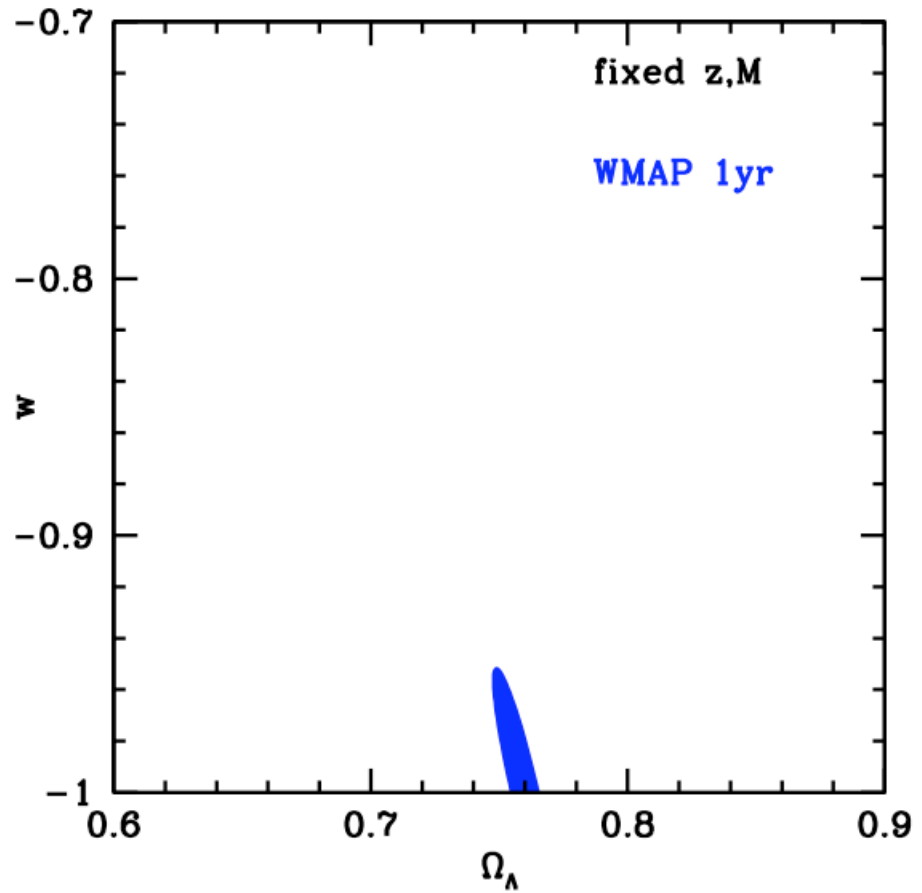


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Baseline constraints

Fixed Mass, Redshifts.

WMAP 1yr





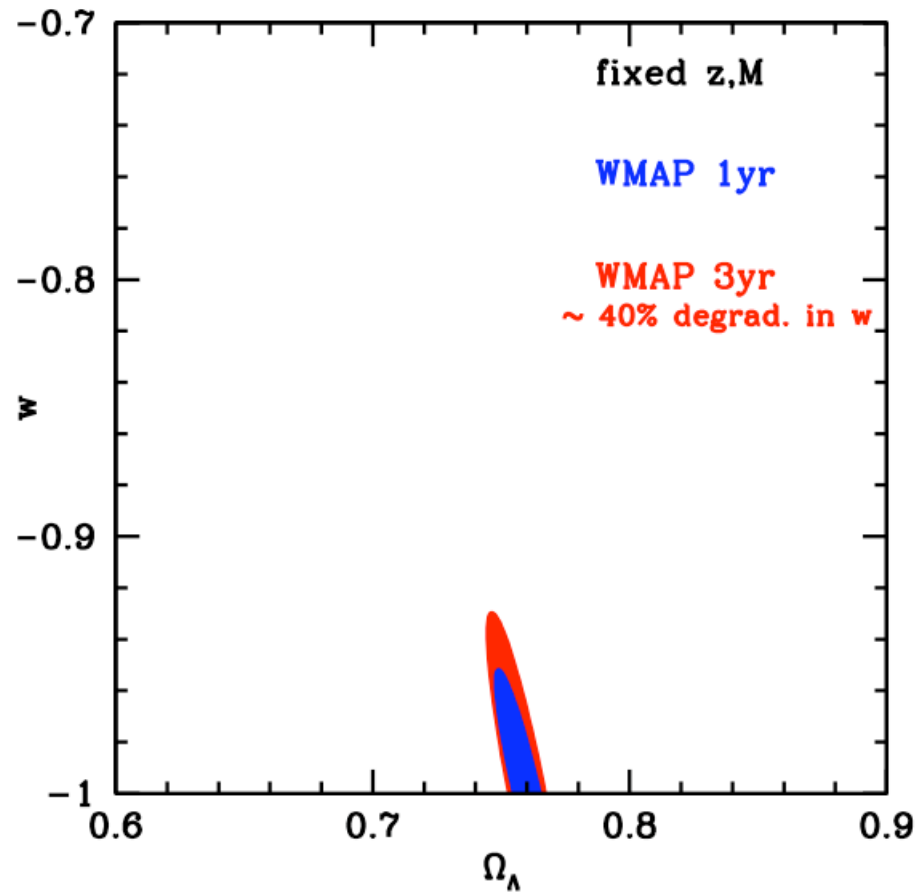
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Baseline constraints

Fixed Mass, Redshifts.

WMAP 1yr

WMAP 3yr

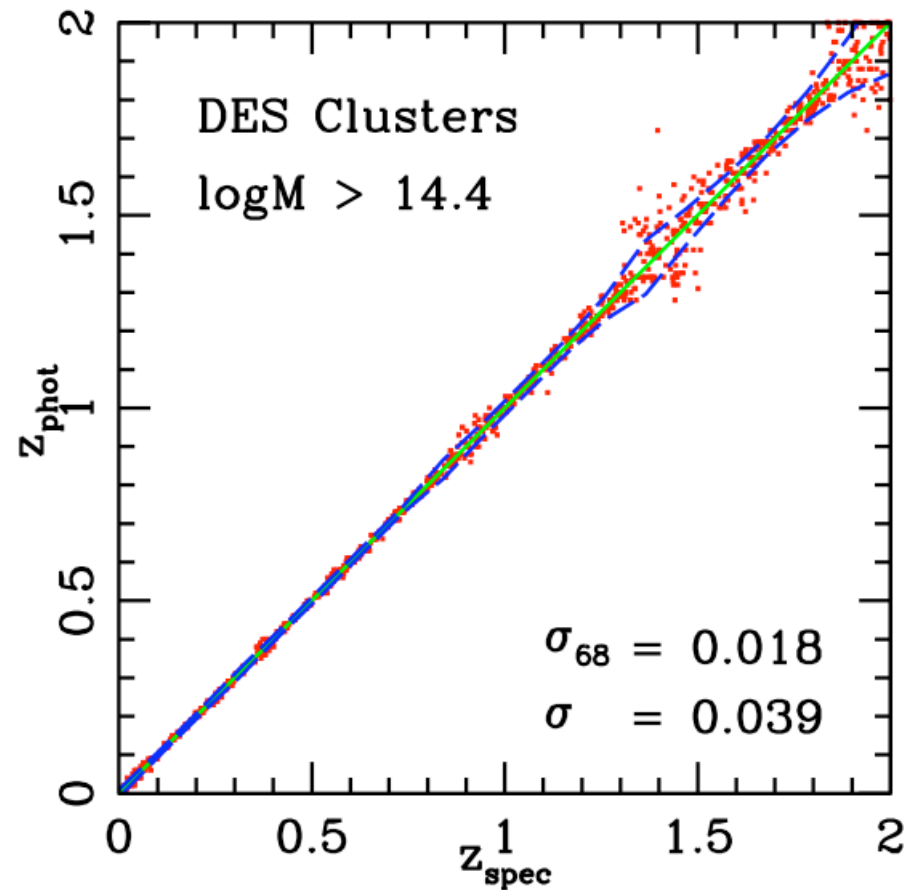
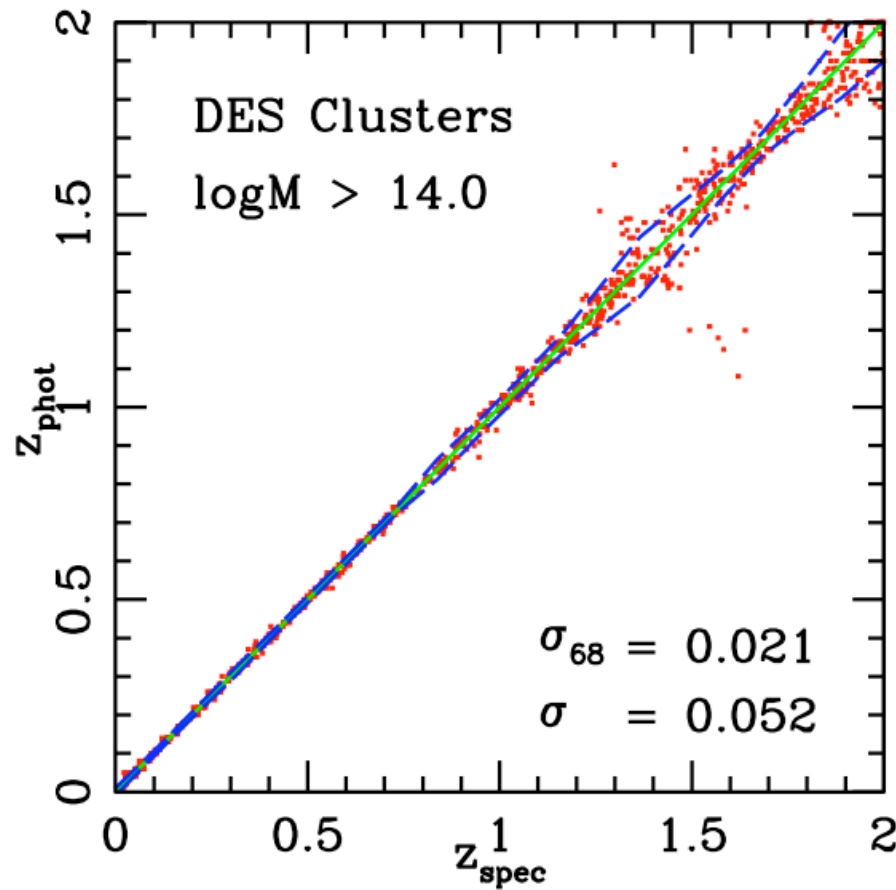




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Cluster Photo-z's

- Huan Lin's catalog. Template Fitting photo-z's

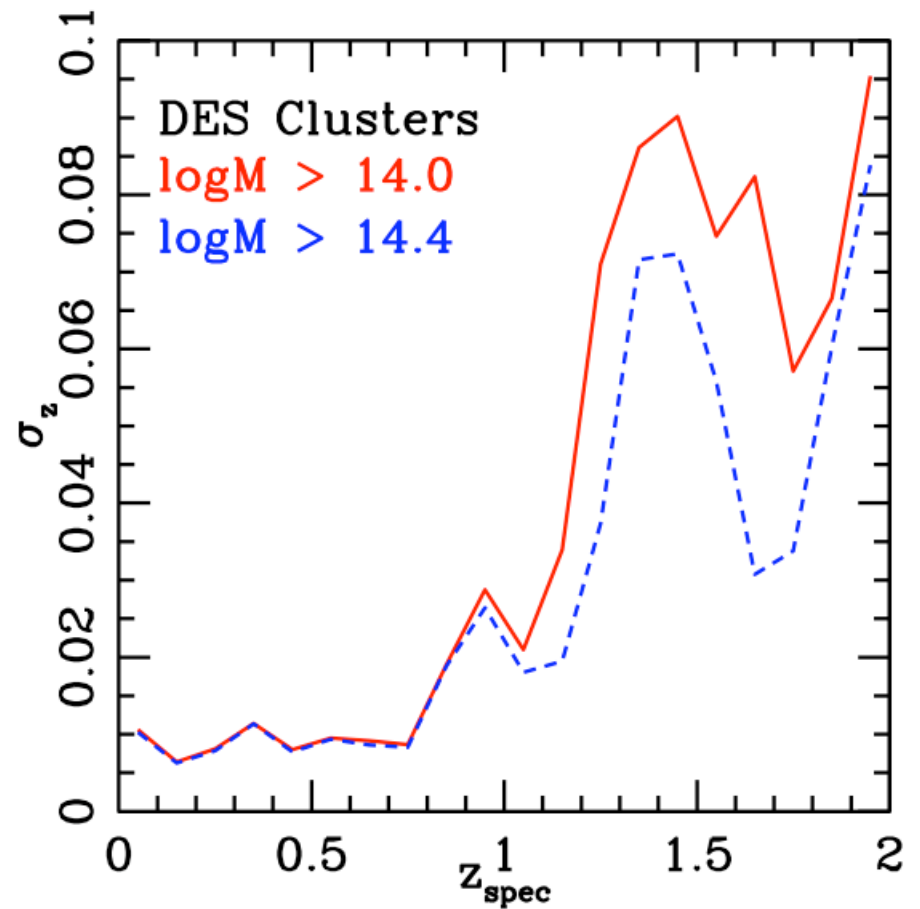
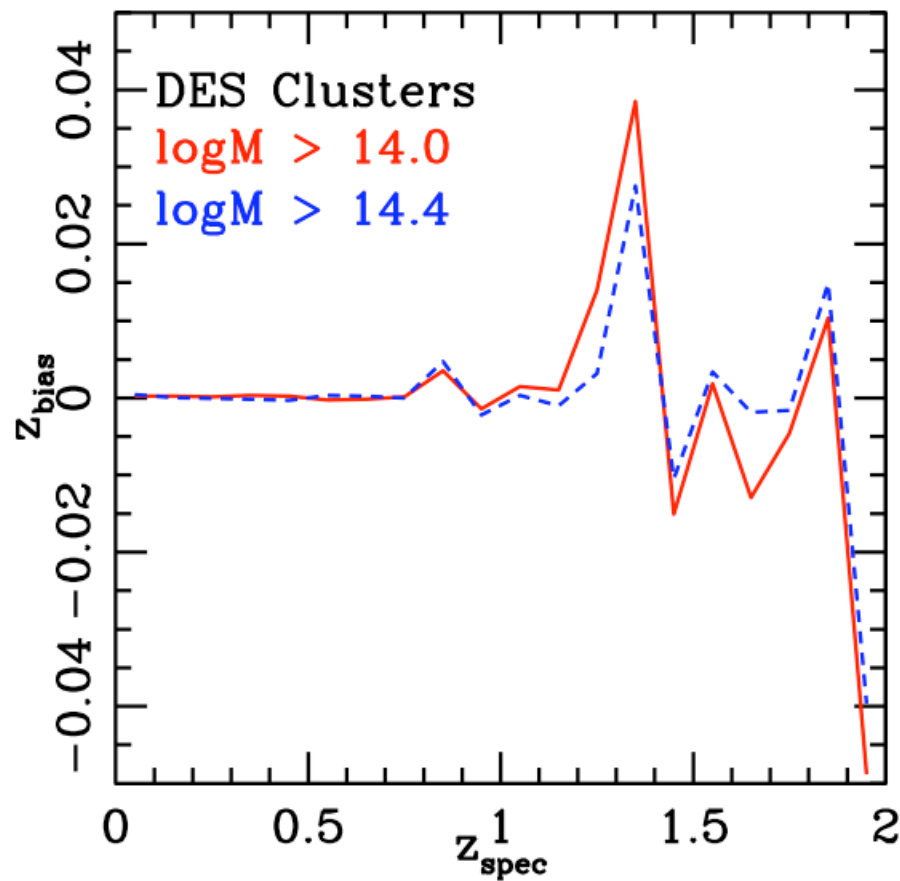




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Cluster Photo-zs

- Huan Lin's catalog. Template Fitting photo-z's





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Constraints

- SPT like, 4000 deg^2 , $z_{\text{max}} = 2$, $\Delta z = 0.1$
 $M_{\text{th}} = 10^{14.2}$ solar masses
- Flat universe
- WMAP 3yr cosmology
- Other cosmological parameters (not DE):
priors of $\sim 1\%$
- Constant w

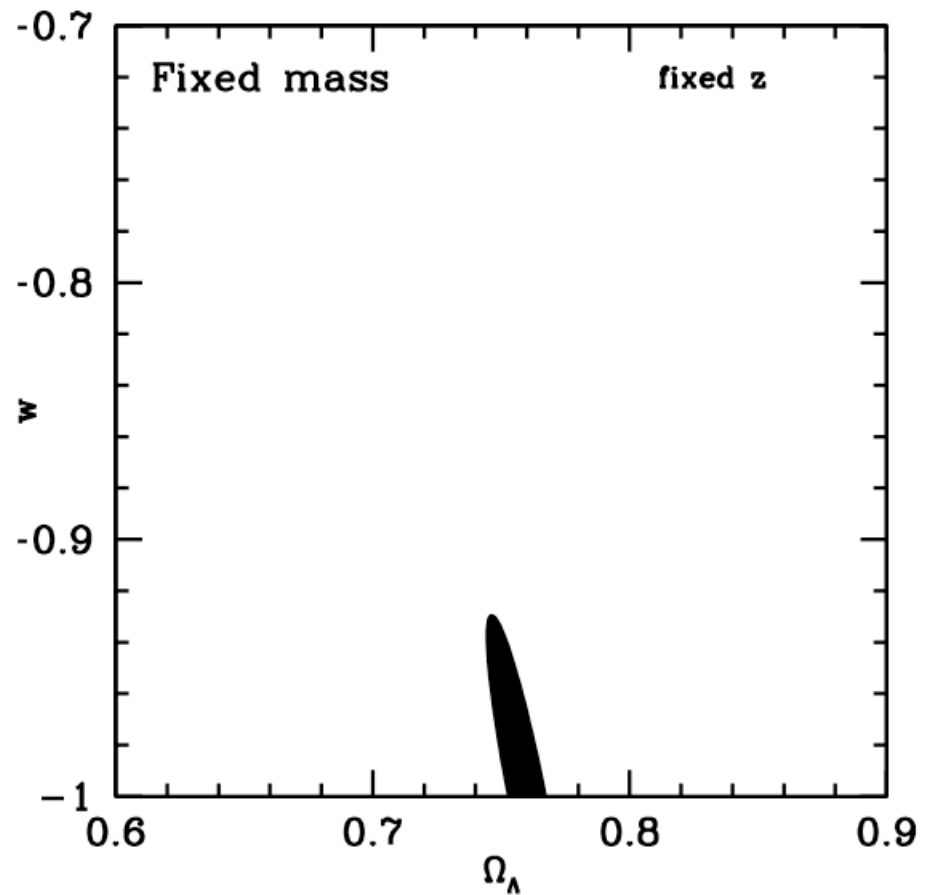


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Fixed Mass-Observable

- Fixed z bias
- Fixed z scatter

- Counts

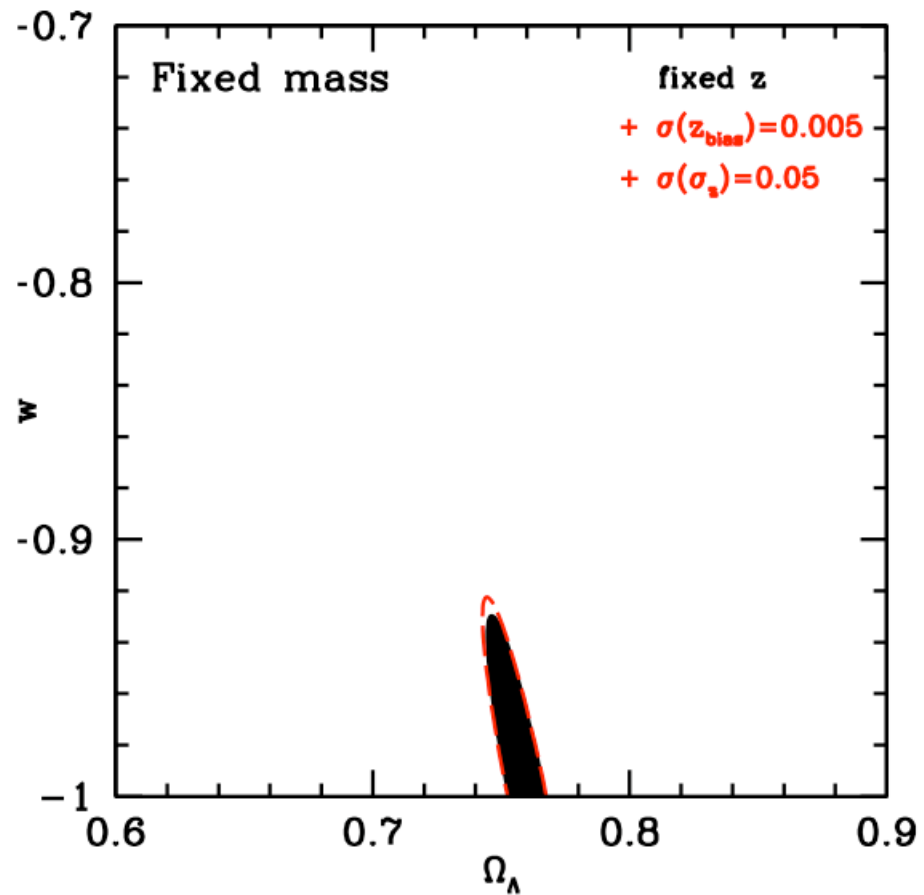




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Fixed Mass-Observable

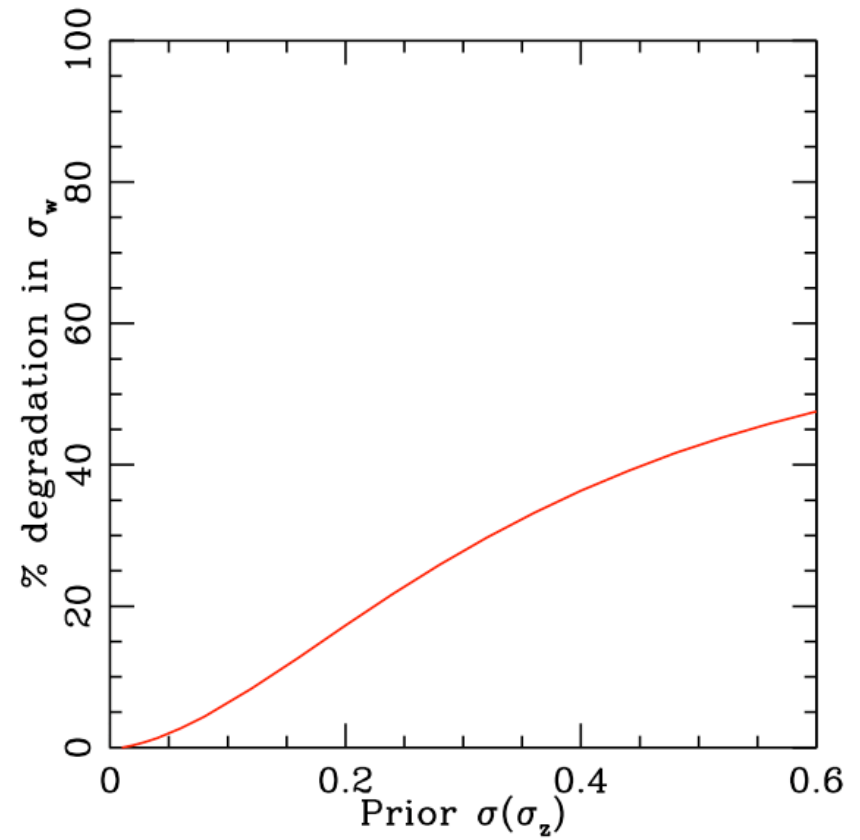
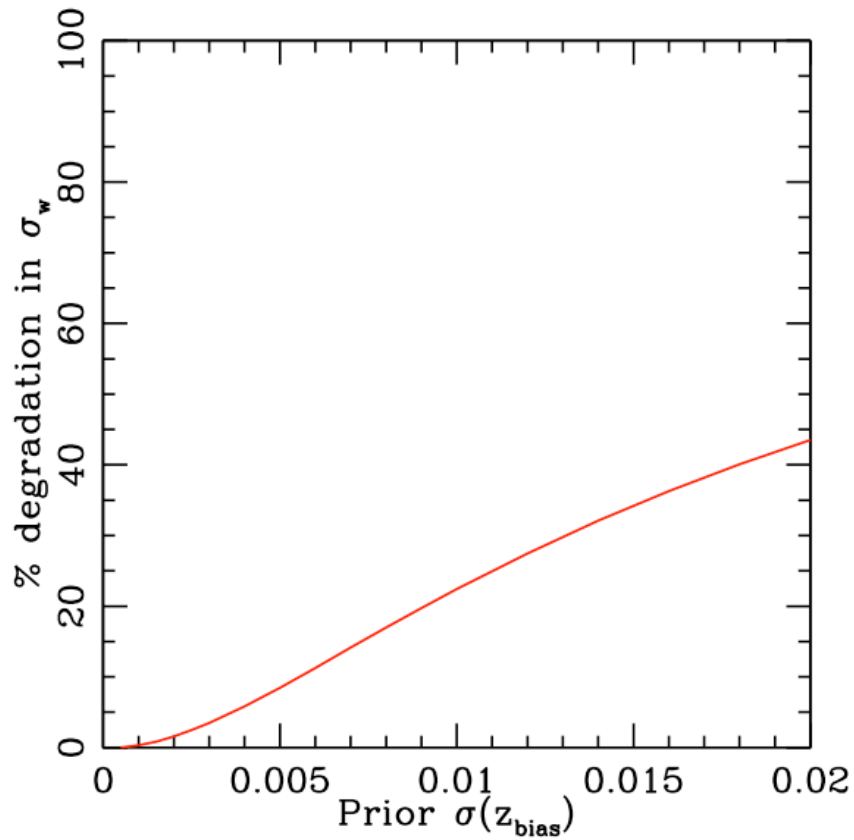
- Prioired z bias
- Prioired z scatter
- Counts





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Fixed Mass-Observable: Degradation in w

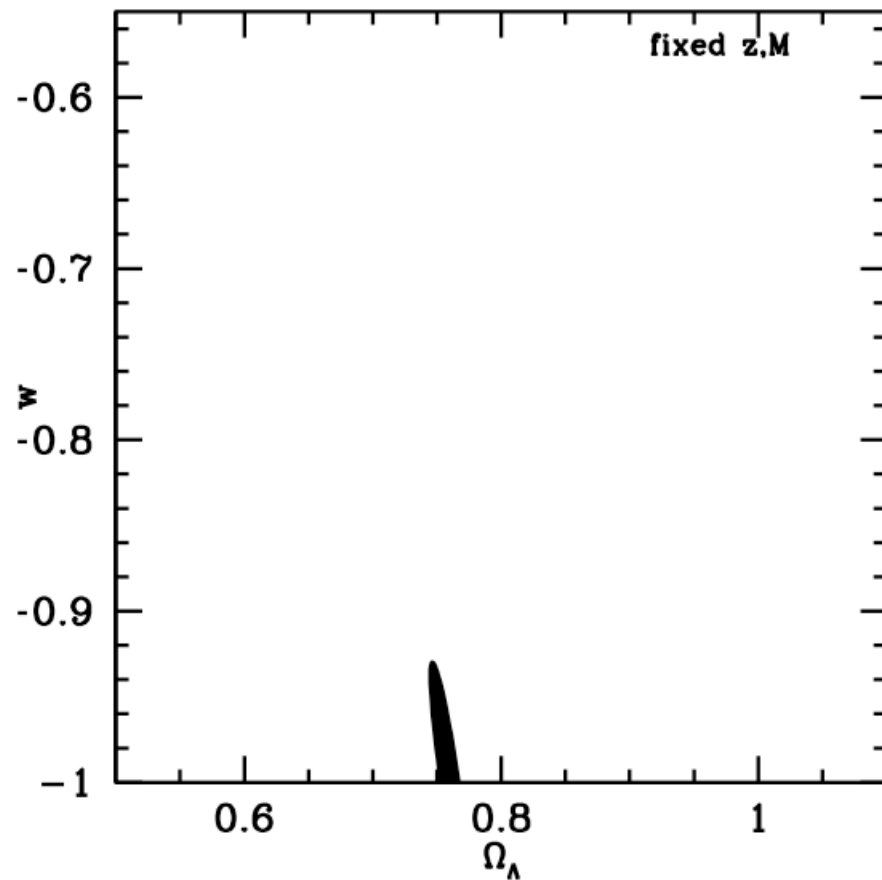




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Self-Calibration: Mean + Scatter in Mass-Observable

- Fixed z bias
- Fixed z scatter
- Fixed M bias
- Fixed M scatter
- Counts

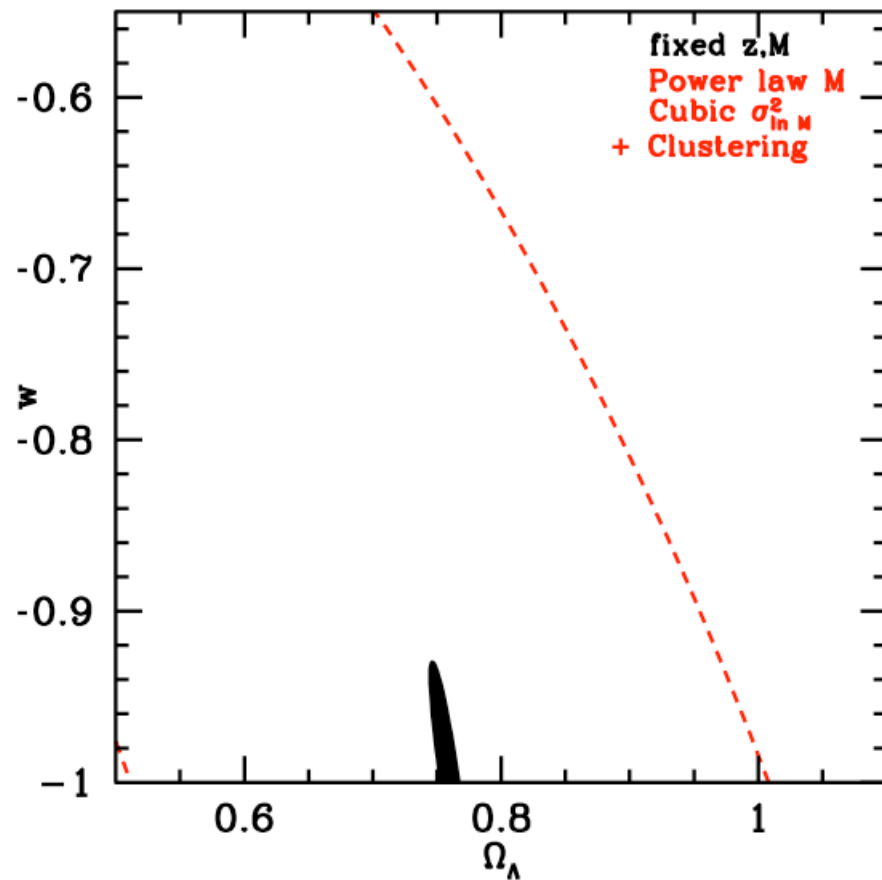




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Self-Calibration: Mean + Scatter in Mass-Observable

- Fixed z bias
- Fixed z scatter
- Power Law M bias
- Cubic M scatter
- Counts
- + Clustering

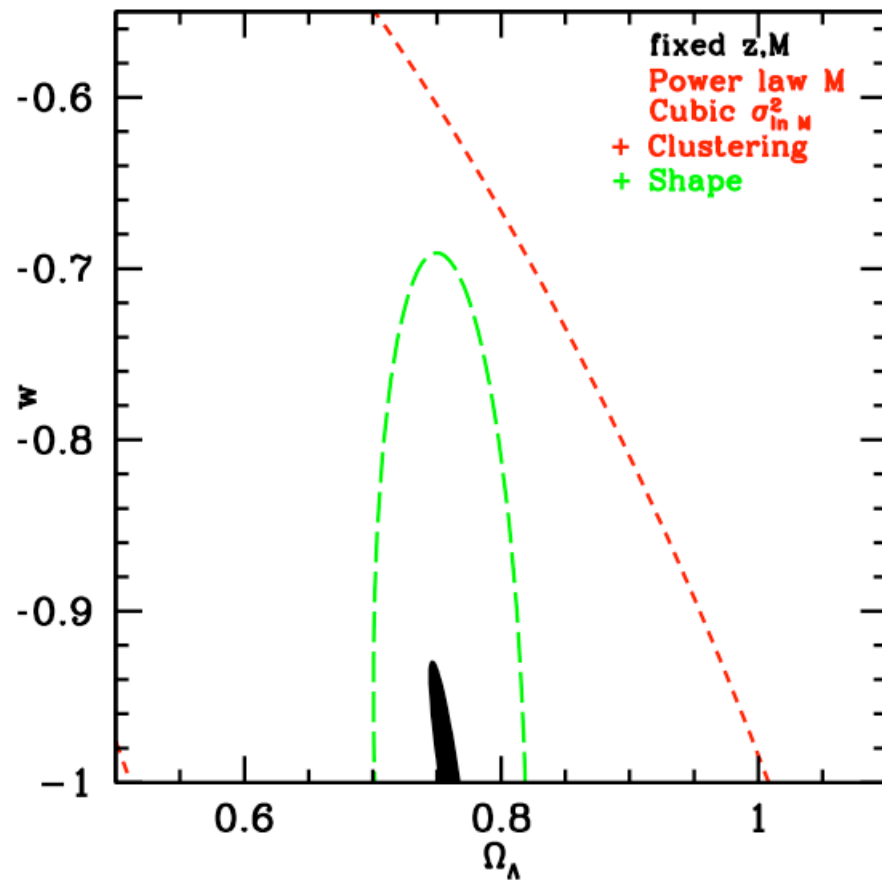




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Self-Calibration: Mean + Scatter in Mass-Observable

- Fixed z bias
- Fixed z scatter
- Power Law M bias
- Cubic M scatter
- Counts
- + Clustering
- + Shape

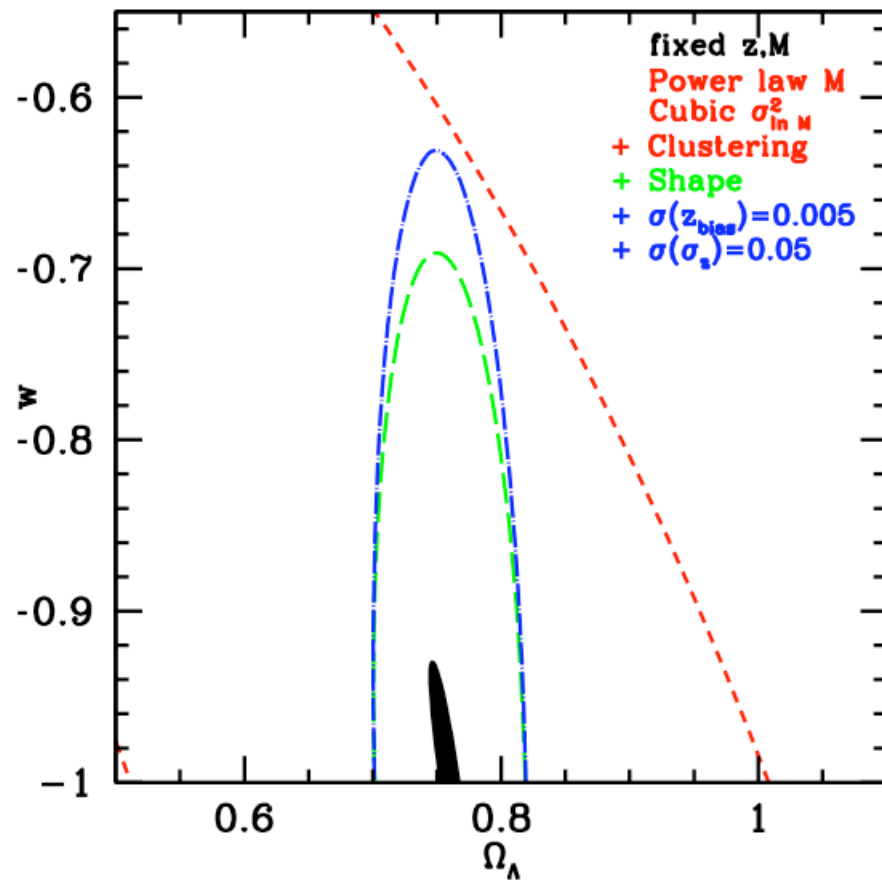




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Self-Calibration: Mean + Scatter in Mass-Observable

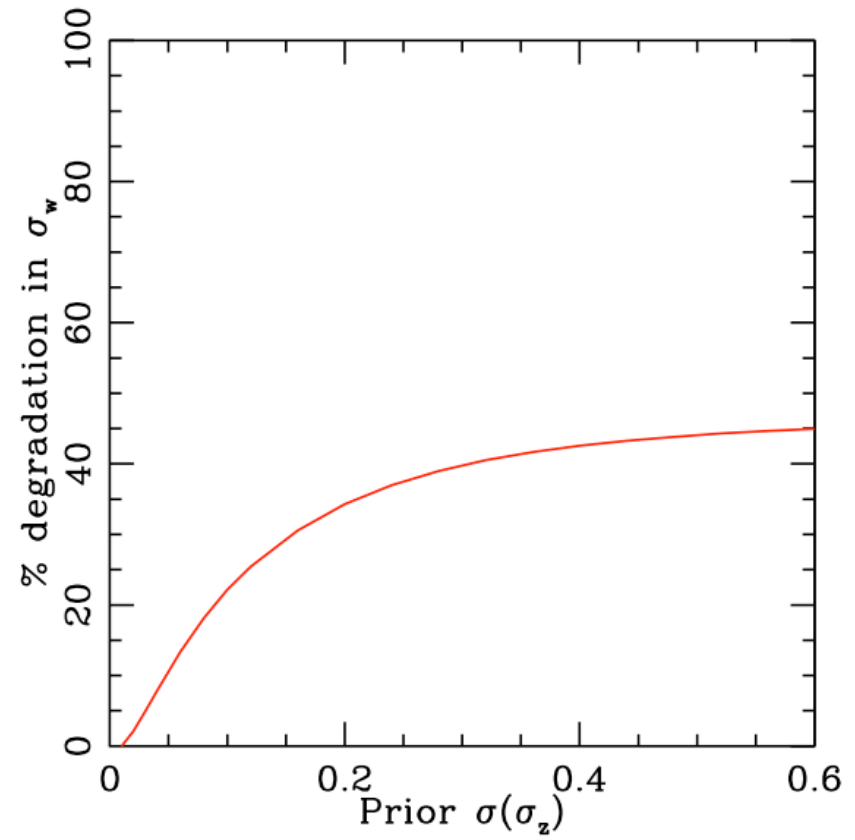
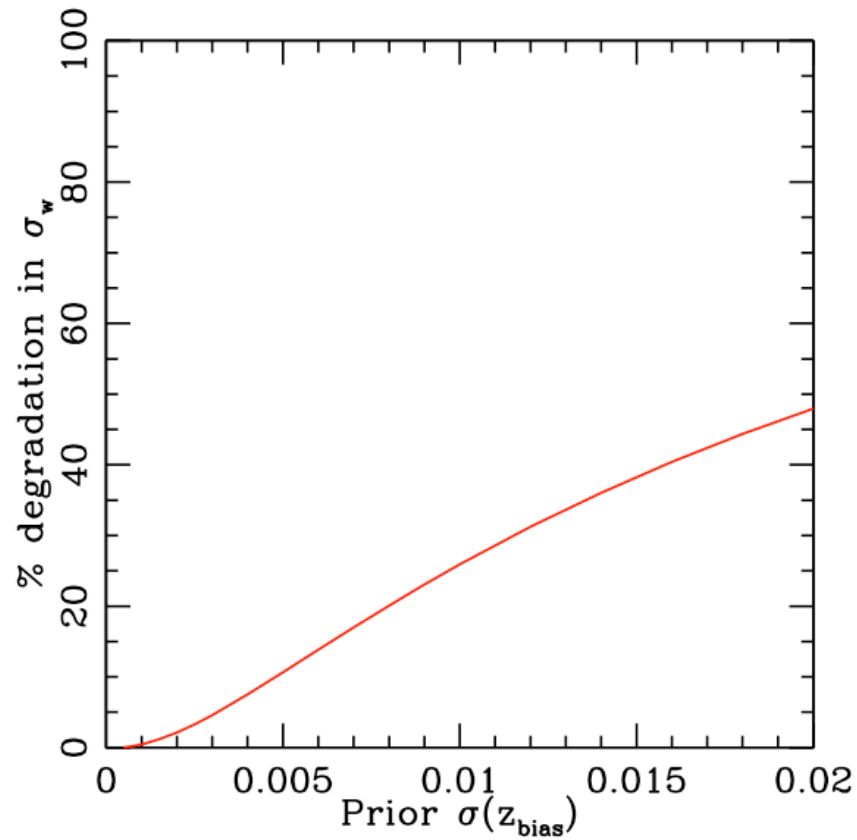
- Prioired z bias
- Prioired z scatter
- Power Law M bias
- Cubic M scatter
- Counts
 - + Clustering
 - + Shape





Mean + Scatter in Mass-Observable: Degradation in w

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Another case: n fixed

- Mean relation: Power law

$$\frac{M(z_i)}{M_{fid}} = e^A (1 + z_i)^n \left(\frac{O}{O_{fid}} \right)^p$$

Assume p fixed.

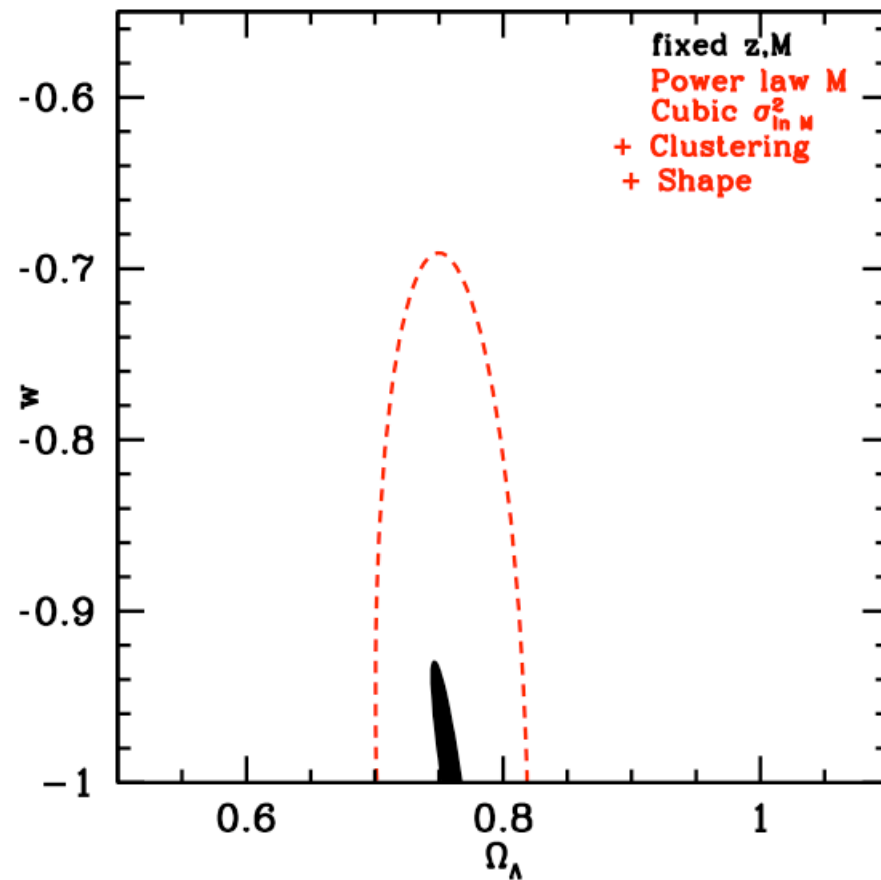
Assume n fixed.



Another case: n fixed

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- Fixed z bias
- Fixed z scatter
- Power Law M bias
- Cubic M scatter
- Counts
- + Clustering
- + Shape

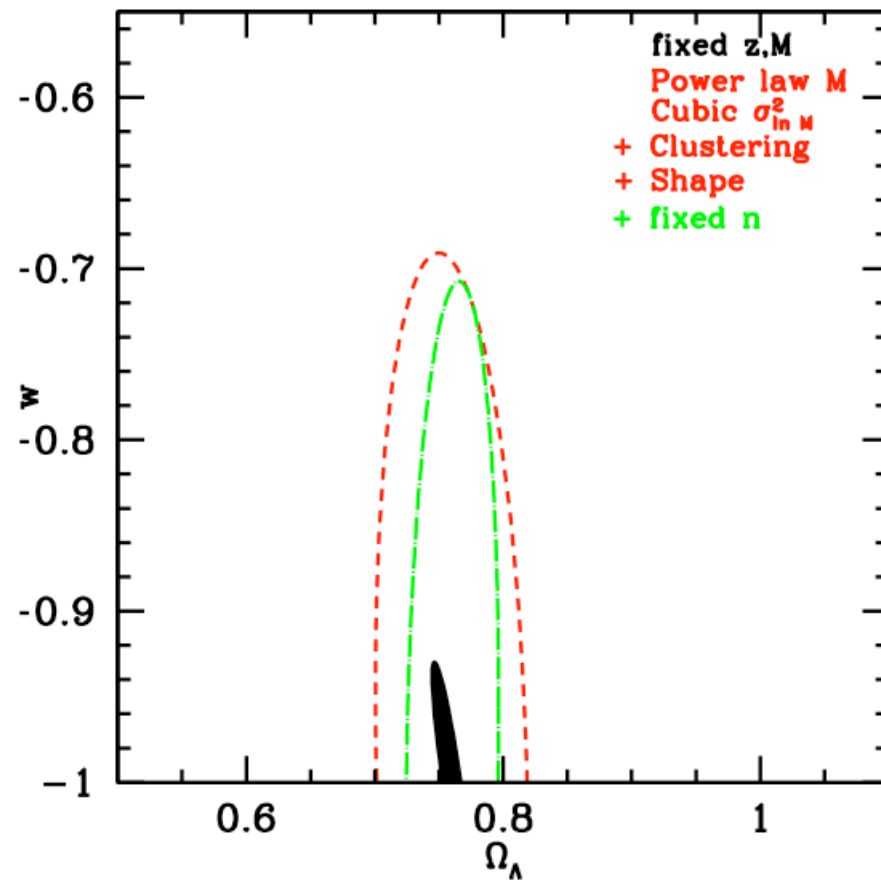




Another case: n fixed

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- Fixed z bias
- Fixed z scatter
- Power Law M bias
- Cubic M scatter
- Counts
 - + Clustering
 - + Shape
 - + n fixed

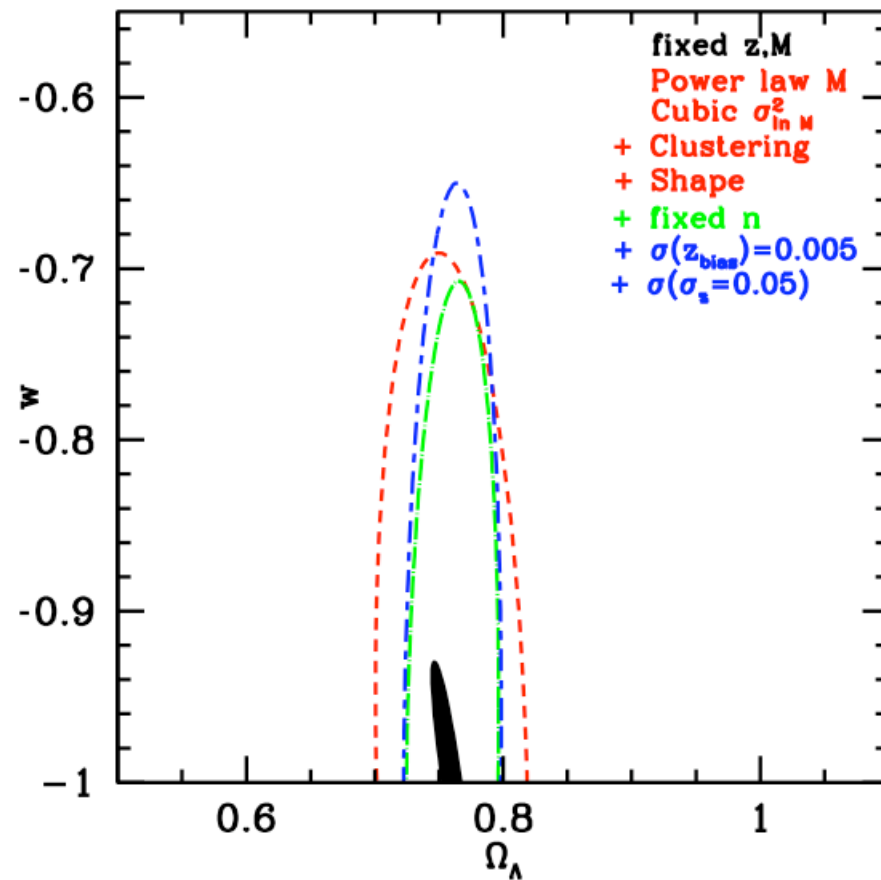




Another case: n fixed

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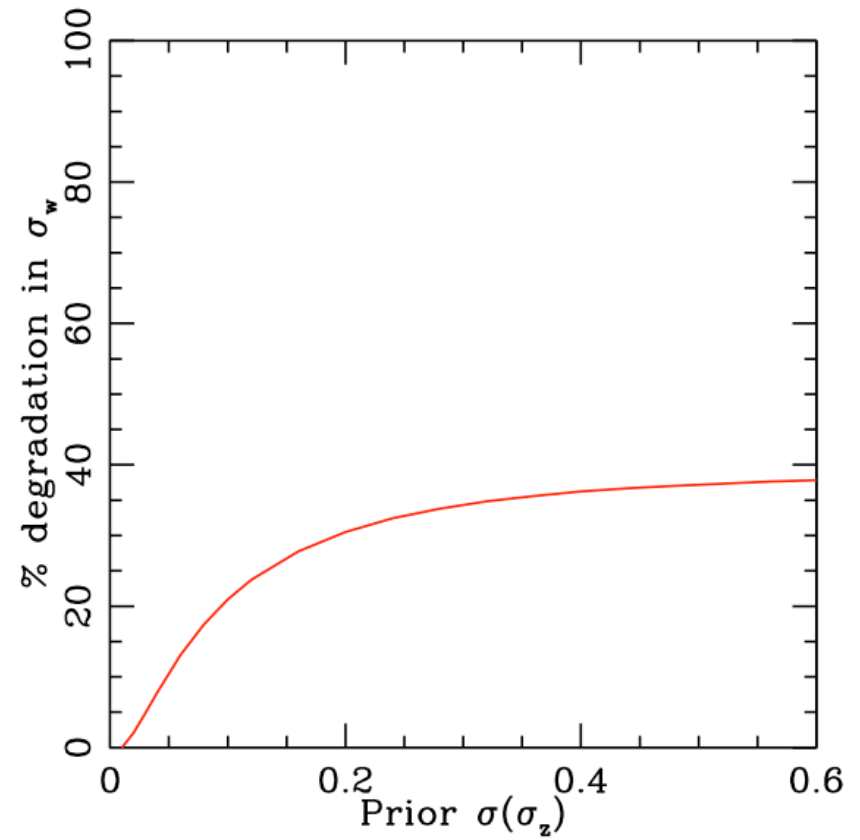
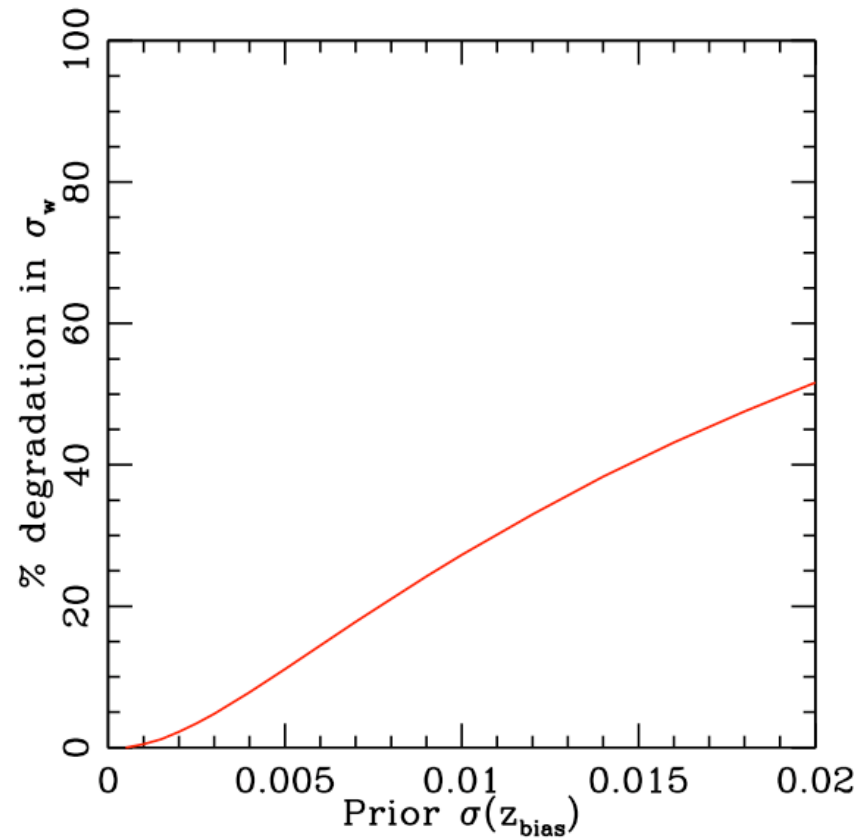
- Prioired z bias
- Prioired z scatter
- Power Law M bias
- Cubic M scatter
- Counts
 - + Clustering
 - + Shape
 - + n fixed





Another case: n fixed

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Summary

- WMAP 3yr: 4 times less clusters
~ 40% degradation in baseline.
Up to ~ 100% in self-calibration.
- Photo-z requirements: ~ 0.005 for z bias,
~ 0.05 for z scatter.
- Future: - Improve uncertainty in z bias and scatter
requirement to be a function of z.
- Calculations with CatSim1 cluster catalog.