Dark Energy Survey Year 1 Results: Galaxy clustering for combined probes

J. Elvin-Poole,¹ M. Crocce,² A. J. Ross,³ T. Giannantonio,^{4,5,6} E. Rozo,⁷ E. S. Rykoff,^{8,9} S. Avila,^{10,11} N. Banik,^{12,13} J. Blazek,^{14,3} S. L. Bridle,¹ R. Cawthon,¹⁵ A. Drlica-Wagner,¹² O. Friedrich,^{6,16} N. Kokron,^{17,18} E. Krause,⁹ N. MacCrann,^{3, 19} J. Prat,²⁰ C. Sánchez,²⁰ L. F. Secco,²¹ I. Sevilla-Noarbe,¹⁰ M. A. Troxel,^{3, 19} T. M. C. Abbott,²² F. B. Abdalla,^{23, 24} S. Allam,¹² J. Annis,¹² J. Asorey,^{25, 26} K. Bechtol,²⁷ M. R. Becker,^{9, 28} A. Benoit-Lévy,^{23, 29, 30} G. M. Bernstein,²¹ E. Bertin,^{30, 29} D. Brooks,²³ E. Buckley-Geer,¹² D. L. Burke,^{8, 9} A. Carnero Rosell,^{31,18} D. Carollo,^{26,32} M. Carrasco Kind,^{33,34} J. Carretero,²⁰ F. J. Castander,² C. E. Cunha,⁹ C. B. D'Andrea,²¹ L. N. da Costa,^{18,31} T. M. Davis,^{25,26} C. Davis,⁹ S. Desai,³⁵ H. T. Diehl,¹² J. P. Dietrich,^{36,37} S. Dodelson,^{12, 15} P. Doel,²³ T. F. Eifler,^{38, 39} A. E. Evrard,^{40, 41} E. Fernandez,²⁰ B. Flaugher,¹² P. Fosalba,² J. Frieman,^{12,15} J. García-Bellido,⁴² E. Gaztanaga,² D. W. Gerdes,^{41,40} K. Glazebrook,⁴³ D. Gruen,^{8,9} R. A. Gruendl,^{33,34} J. Gschwend,^{31,18} G. Gutierrez,¹² W. G. Hartley,^{23,44} S. R. Hinton,²⁵ K. Honscheid,^{3, 19} J. K. Hoormann,²⁵ B. Jain,²¹ D. J. James,⁴⁵ M. Jarvis,²¹ T. Jeltema,⁴⁶ M. W. G. Johnson,³³ M. D. Johnson,³³ A. King,²⁵ K. Kuehn,⁴⁷ S. Kuhlmann,⁴⁸ N. Kuropatkin,¹² O. Lahav,²³ G. Lewis,^{49,26} T. S. Li,¹² C. Lidman,^{47,26} M. Lima,^{17,18} H. Lin,¹² E. Macaulay,²⁵ M. March,²¹ J. L. Marshall,⁵⁰ P. Martini,^{3,51}
 P. Melchior,⁵² F. Menanteau,^{34,33} R. Miquel,^{20,53} J. J. Mohr,^{16,37,36} A. Möller,^{54,26} R. C. Nichol,¹¹ B. Nord,¹² C. R. O'Neill,^{25,26} W.J. Percival,¹¹ D. Petravick,³³ A. A. Plazas,³⁹ A. K. Romer,^{55,8} M. Sako,²¹ E. Sanchez,¹⁰ V. Scarpine,¹² R. Schindler,⁸ M. Schubnell,⁴¹ E. Sheldon,⁵⁶ M. Smith,⁵⁷ R. C. Smith,²² M. Soares-Santos,¹² F. Sobreira,^{18,58} N. E. Sommer,^{54,26} E. Suchyta,⁵⁹ M. E. C. Swanson,³³ G. Tarle,⁴¹ D. Thomas,^{11, 19} B. E. Tucker,^{26, 54} D. L. Tucker,¹² S. A. Uddin,^{26, 60} V. Vikram,⁴⁸ A. R. Walker,²² R. H. Wechsler,^{8, 28, 9} J. Weller,^{36, 16, 6} W. Wester,¹² R. C. Wolf,²¹ F. Yuan,^{26, 54} B. Zhang,^{54, 26} and J. Zuntz⁶¹

(DES Collaboration)

¹Jodrell Bank Center for Astrophysics, School of Physics and Astronomy,

University of Manchester, Oxford Road, Manchester, M13 9PL, UK

²Institute of Space Sciences, IEEC-CSIC, Campus UAB,

Carrer de Can Magrans, s/n, 08193 Barcelona, Spain

³Center for Cosmology and Astro-Particle Physics,

The Ohio State University, Columbus, OH 43210, USA

⁴Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK

⁵Kavli Institute for Cosmology, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK

⁶ Universitäts-Sternwarte, Fakultät für Physik, Ludwig-Maximilians

Universität München, Scheinerstr. 1, 81679 München, Germany

⁷Department of Physics, University of Arizona, Tucson, AZ 85721, USA

⁸SLAC National Accelerator Laboratory, Menlo Park, CA 94025, USA

⁹Kavli Institute for Particle Astrophysics & Cosmology,

P. O. Box 2450, Stanford University, Stanford, CA 94305, USA

¹⁰Centro de Investigaciones Energéticas, Medioambientales y Tecnológicas (CIEMAT), Madrid, Spain

¹¹Institute of Cosmology & Gravitation, University of Portsmouth, Portsmouth, PO1 3FX, UK

¹²Fermi National Accelerator Laboratory, P. O. Box 500, Batavia, IL 60510, USA

¹³Department of Physics, University of Florida, Gainesville, Florida 32611, USA

¹⁴Institute of Physics, Laboratory of Astrophysics,

École Polytechnique Fédérale de Lausanne (EPFL),

Observatoire de Sauverny, 1290 Versoix, Switzerland

¹⁵Kavli Institute for Cosmological Physics, University of Chicago, Chicago, IL 60637, USA

¹⁶Max Planck Institute for Extraterrestrial Physics, Giessenbachstrasse, 85748 Garching, Germany

¹⁷Departamento de Física Matemática, Instituto de Física,

Universidade de São Paulo, CP 66318, São Paulo, SP, 05314-970, Brazil

¹⁸Laboratório Interinstitucional de e-Astronomia - LIneA,

Rua Gal. José Cristino 77, Rio de Janeiro, RJ - 20921-400, Brazil

¹⁹Department of Physics, The Ohio State University, Columbus, OH 43210, USA

²⁰Institut de Física d'Altes Energies (IFAE), The Barcelona Institute of Science and Technology,

Campus UAB, 08193 Bellaterra (Barcelona) Spain

²¹Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, PA 19104, USA

²²Cerro Tololo Inter-American Observatory, National Optical Astronomy Observatory, Casilla 603, La Serena, Chile

²³Department of Physics & Astronomy, University College London, Gower Street, London, WC1E 6BT, UK

²⁴Department of Physics and Electronics, Rhodes University, PO Box 94, Grahamstown, 6140, South Africa

²⁵School of Mathematics and Physics, University of Queensland, Brisbane, QLD 4072, Australia

²⁶ARC Centre of Excellence for All-sky Astrophysics (CAASTRO)

²⁷LSST, 933 North Cherry Avenue, Tucson, AZ 85721, USA

²⁸Department of Physics, Stanford University, 382 Via Pueblo Mall, Stanford, CA 94305, USA

²⁹CNRS, UMR 7095, Institut d'Astrophysique de Paris, F-75014, Paris, France

³⁰Sorbonne Universités, UPMC Univ Paris 06, UMR 7095,

Institut d'Astrophysique de Paris, F-75014, Paris, France

³¹Observatório Nacional, Rua Gal. José Cristino 77, Rio de Janeiro, RJ - 20921-400, Brazil

³²INAF - Osservatorio Astrofisico di Torino, Pino Torinese, Italy

³³National Center for Supercomputing Applications, 1205 West Clark St., Urbana, IL 61801, USA

³⁴Department of Astronomy, University of Illinois, 1002 W. Green Street, Urbana, IL 61801, USA

³⁵ Department of Physics, IIT Hyderabad, Kandi, Telangana 502285, India

³⁶Excellence Cluster Universe, Boltzmannstr. 2, 85748 Garching, Germany

³⁷Faculty of Physics, Ludwig-Maximilians-Universität, Scheinerstr. 1, 81679 Munich, Germany

³⁸Department of Physics, California Institute of Technology, Pasadena, CA 91125, USA

³⁹ Jet Propulsion Laboratory, California Institute of Technology,

4800 Oak Grove Dr., Pasadena, CA 91109, USA

⁴⁰Department of Astronomy, University of Michigan, Ann Arbor, MI 48109, USA

⁴¹Department of Physics, University of Michigan, Ann Arbor, MI 48109, USA

⁴²Instituto de Fisica Teorica UAM/CSIC, Universidad Autonoma de Madrid, 28049 Madrid, Spain

⁴³Centre for Astrophysics & Supercomputing, Swinburne University of Technology, Victoria 3122, Australia

⁴⁴Department of Physics, ETH Zurich, Wolfgang-Pauli-Strasse 16, CH-8093 Zurich, Switzerland

⁴⁵Astronomy Department, University of Washington, Box 351580, Seattle, WA 98195, USA

⁴⁶Santa Cruz Institute for Particle Physics, Santa Cruz, CA 95064, USA

⁴⁷Australian Astronomical Observatory, North Ryde, NSW 2113, Australia

⁴⁸Argonne National Laboratory, 9700 South Cass Avenue, Lemont, IL 60439, USA

⁴⁹Sydney Institute for Astronomy, School of Physics,

A28, The University of Sydney, NSW 2006, Australia

⁵⁰George P. and Cynthia Woods Mitchell Institute for Fundamental Physics and Astronomy,

and Department of Physics and Astronomy, Texas A&M University, College Station, TX 77843, USA

⁵¹Department of Astronomy, The Ohio State University, Columbus, OH 43210, USA

⁵²Department of Astrophysical Sciences, Princeton University, Peyton Hall, Princeton, NJ 08544, USA

⁵³Institució Catalana de Recerca i Estudis Avançats, E-08010 Barcelona, Spain

⁵⁴ The Research School of Astronomy and Astrophysics,

Australian National University, ACT 2601, Australia

⁵⁵Department of Physics and Astronomy, Pevensey Building, University of Sussex, Brighton, BN1 9QH, UK ⁵⁶Brookhaven National Laboratory, Bldg 510, Upton, NY 11973, USA

⁵⁷School of Physics and Astronomy, University of Southampton, Southampton, SO17 1BJ, UK

School of Physics and Astronomy, University of Southampton, Southampton, SOIT IBJ, UK

⁵⁸Instituto de Física Gleb Wataghin, Universidade Estadual de Campinas, 13083-859, Campinas, SP, Brazil

⁵⁹Computer Science and Mathematics Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831

⁶⁰Purple Mountain Observatory, Chinese Academy of Sciences, Nanjing, Jiangshu 210008, China

⁶¹Institute for Astronomy, University of Edinburgh, Edinburgh EH9 3HJ, UK

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We measure the clustering of DES Year 1 galaxies that are intended to be combined with weak lensing samples in order to produce precise cosmological constraints from the joint analysis of largescale structure and lensing correlations. Two-point correlation functions are measured for a sample of 6.6×10^5 luminous red galaxies selected using the REDMAGIC algorithm over an area of 1321 square degrees, in the redshift range 0.15 < z < 0.9, split into five tomographic redshift bins. The sample has a mean redshift uncertainty of $\sigma_z/(1+z) = 0.017$. We quantify and correct spurious correlations induced by spatially variable survey properties, testing their impact on the clustering measurements and covariance. We demonstrate the sample's robustness by testing for stellar contamination, for potential biases that could arise from the systematic correction, and for the consistency between the two-point auto- and cross-correlation functions. We show that the corrections we apply have a significant impact on the resultant measurement of cosmological parameters, but that the results are robust against arbitrary choices in the correction method. We find the linear galaxy bias in each redshift bin in a fiducial cosmology to be $b(z=0.24) = 1.40 \pm 0.08, b(z=0.38) = 1.61 \pm 0.05$, $b(z=0.53) = 1.60 \pm 0.04$ for galaxies with luminosities $L/L_* > 0.5$, $b(z=0.68) = 1.93 \pm 0.05$ for $L/L_* > 1$ and $b(z=0.83) = 1.99 \pm 0.07$ for $L/L_* > 1.5$, broadly consistent with expectations for the redshift and luminosity dependence of the bias of red galaxies. We show these measurements to be consistent with the linear bias obtained from tangential shear measurements.

I. INTRODUCTION

Galaxies are a biased tracer of the matter density field. In the standard 'halo model' paradigm, they form in collapsed over-densities (dark matter halos; [1]), and the mass of the halo they reside in is known to correlate with the luminosity and color of the galaxy, with more luminous and redder galaxies strongly correlated with higher mass. Therefore, the galaxy 'bias' depends strongly on the particular sample being studied. Thus, in cosmological studies the galaxy bias is often treated as a nuisance parameter — one that is degenerate with the amplitude of the clustering of matter. See, e.g., [2] and references therein.

The degeneracy can be broken with additional observables. This includes the weak gravitational lensing 'shear' field, which is induced by the matter density field. Correlation between the galaxies and the shear field ([3]; often referred to as 'galaxy-galaxy lensing') contains one factor of the galaxy bias and two factors of the matter field. The galaxy auto-correlation contains two factors of the galaxy bias and again two factors of the matter field. Thus, the combination of the two measurements can break the degeneracy between the two quantities, and it is a sensitive probe of the late-time matter field (see, e.g., [4, 5])

The auto-correlation of the shear field alone includes no factors of the galaxy bias and can thus be used directly as a probe of the matter field. However, its sensitivity to many systematic uncertainties related to the estimation of the shear field differs from that of the galaxy-galaxy lensing signal. As shown by [6–9], the impact of such systematic uncertainties can be mitigated by combining the shear auto-correlation measurements with those of galaxy clustering and galaxy-galaxy lensing. Thus there is substantial gain to be obtained from a combined analysis.

Such a combined analysis is performed with the Dark Energy Survey (DES[10]; [11]) Year-1 (Y1) data ([12]; hereafter Y1COSMO). DES is an imaging survey currently amassing data over a 5000 deg² footprint in five passbands (grizY). When completed, it will have mapped 300 million galaxies and tens of thousands of galaxy clusters.

In this work, we study the clustering of red sequence galaxies selected from DES Y1 data using the RED-MAGIC [13] algorithm. We study the same sample used to obtain cosmological results in the Y1COSMO combined analysis. In particular, we study the large-scale clustering amplitude and its sensitivity to observational systematics. Following previous studies [14–17], we use angular maps to track the observing conditions of the Y1 data in order to identify and correct for spurious fluctuations in the galaxy density field. We further determine the effect the corrections have on the covariance matrix of the angular auto-correlation of the galaxies. We present robust measurements of the clustering amplitude of RED-MAGIC galaxies as a function of redshift and luminosity, thus gaining insight into the physical nature of these galaxies and how they compare to other red galaxy samples. The results of this paper are then used for the joint DES cosmological analysis presented in Y1COSMO.

This outline of this paper is: we summarize in Section II the model we use to describe our galaxy clustering measurements; we present in Section III the DES data we use; Section IV presents how we measure clustering statistics and estimate their covariance; Section V summarizes the results of our observational systematic tests. We present our primary results with galaxy bias measurements in Section VI and a demonstration of their robustness in Section VII before concluding in Section VIII.

In order to avoid confirmation bias, we have performed this analysis "blind": we did not measure parameter constraints or plot the correlation function measured from the data on the same axis as any theoretical prediction or simulated clustering measurement until the sample and all measurements in Y1COSMO were finalized.

Unless otherwise noted, we use a fiducial Λ CDM cosmology, fixing cosmological parameters at $\Omega_m = 0.295$, $A_s = 2.260574 \times 10^{-9}$, $\Omega_b = 0.0468$, h = 0.6881, $n_s = 0.9676$. This is consistent with the latest cosmological data from the Planck mission [18] and is used as the fiducial cosmology for all the DES Y1 analyses used in Y1COSMO. We use this cosmology to generate Gaussian mocks in Section V for systematics testing.

After un-blinding, we re-measure the galaxy bias, fixing the cosmological parameters at the mean of the DES Y1COSMO posterior, $\Omega_m = 0.2276$, $A_s = 2.667454 \times 10^{-9}$, $\Omega_b = 0.0526$, h = 0.7619, $n_s = 0.9964$ (note that we show these values at a greater precision than can be measured by DES). This cosmology was used for all bias measurements in Section VI.

II. THEORY

Throughout this paper we model REDMAGIC clustering measurements assuming a local, linear galaxy bias model [19], where the galaxy and matter density fluctuations are related by $\delta_g(\mathbf{x}) = b\delta_m(\mathbf{x})$, with density fluctuations defined by $\delta \equiv (n(\mathbf{x}) - \bar{n})/\bar{n}$. The validity of this assumption over the scales considered here is provided in [20] and shown in simulations in [21].

We consider multiple galaxy redshift bins i, each characterized by a REDMAGIC galaxy redshift distribution $n_g^i(z)$, normalized to unity in redshift, and a galaxy bias b^i which is assumed to be constant across the redshift bin range. Under the Limber [22] and flat-sky approximation the theoretical prediction for the galaxy correlation function $w(\theta)$ in a given bin is,

$$w^{i}(\theta) = (b^{i})^{2} \int \frac{dl}{l} 2\pi J_{0}(l\theta) \int d\chi$$
$$\times \frac{\left[n_{g}^{i}(z(\chi))\right]^{2}}{\chi^{2}H(z)} P_{\rm NL}\left(\frac{l+1/2}{\chi}, z(\chi)\right), \qquad (1)$$

where the speed of light has been set to one, $\chi(z)$ is the comoving distance to a given redshift (in a flat universe, which is assumed throughout); J_0 is the Bessel function of order zero; H(z) is the Hubble expansion rate at redshift z; and $P_{\rm NL}(k; z)$ is the 3D matter power spectrum at redshift z and wavenumber k (which, in this Limber approximation, is set equal to $(l + 1/2)/\chi$). Note that in Eq. 1 we have assumed the bias to be constant within each bin, see Fig. 8 in [20] for a test of this assumption. Again, all assumptions and approximations mentioned here have been shown to be inconsequential in [20, 21]. To model cross-correlation between redshift bins we simply change $n_{\rm g}^i(z)^2 \rightarrow n_{\rm g}^i(z)n_{\rm g}^j(z)$ and $(b^i)^2 \rightarrow b^i b^j$ in Eq. 1.

Throughout this paper, we use the COSMOSIS framework [23] to compute correlation functions, and to infer cosmological parameters. The evolution of linear density fluctuations is obtained using the CAMB module [24] and then converted to a non-linear matter power spectrum $P_{NL}(k)$ using the updated Halofit recipe [25].

The theory modeling we use assumes the Limber approximation, and it also neglects redshift space distortions. For the samples and redshift binning used in this paper, those effects start to become relevant at scales of $\theta \gtrsim 1 \deg$ [26–28]. In a companion paper [20] it is explicitly shown that they have negligible impact in derived cosmological parameters given the statistical error bars of DES Y1. Concretely a theory data vector was produced with the exact (non-Limber) formula including redshift space distortions and was then analyzed with the baseline pipeline assumed here, and also in Y1COSMO. Figure 8 in [20] shows that including or not including these non-linear contributions make negligible impact in parameters such as Ω_m and S_8 for a LCDM Universe or w in a wCDM one. We also test the impact of these effects on the fixed cosmology bias measurements in Section VI and find them to be negligible. Hence in what follows, such terms are ignored for speed and simplicity. However future data analyses may need to account for these effects due to improved statistical uncertainty.

We model (and marginalize over) photometric redshift bias uncertainties as an additive shift Δz^i in the RED-MAGIC redshift distribution $n_{\rm RM}^i(z)$ for each redshift bin *i*.

$$n^{i}(z) = n^{i}_{\rm RM}(z - \Delta z^{i}) \tag{2}$$

The priors on the Δz^i nuisance parameters, shown in Table II, are described in [29]. We use the same Δz^i as Y1COSMO for all tests of robustness of the parameter constraints.

We also compare the measurements of b^i to the same quantity measured by galaxy-galaxy lensing using the two-point correlation function γ_t (see [30] for definition). We use the notation b^i_{\times} for this measurement. The details of this measurement are described in [30] (hereafter Y1GGL). In order to take the off-diagonal elements of the covariance matrix between the two probes into account, we produce joint constraints from $w(\theta)$ and γ_t at fixed cosmology, using different bias parameters for the two probes, and marginalizing over the same nuisance parameters as were used in the fiducial analysis of Y1COSMO (intrinsic alignments, source photo-z bias, and shear calibration). To test the consistency between the two probes we use the parameter r which is,

$$r^i = \frac{b^i_{\times}}{b^i}.$$
(3)

If $r \neq 1$, this indicates an inconsistency between the two bias measurements and would thus suggest a breakdown of our simple linear bias model. This test informs the choice of fixing r = 1 in the Y1COSMO analysis.

III. DATA

A. Y1 Gold

We use data taken in the first year (Y1) of DES observations [31]. Photometry and 'clean' galaxy samples were produced with this data as outlined by [32] (hereafter denoted 'Y1GOLD'). The outputs of this process represent the Y1 'Gold' catalog. Data were obtained over a total footprint of $\sim 1800 \text{ deg}^2$; this footprint is defined by a HEALPIX [33] map at resolution $N_{\rm side} = 4096$ (equivalent to 0.74 square arcmin) and includes only pixels with minimum exposure time of at least 90 seconds in each of the q,r,i, and z-bands, a valid calibration solution, as well as additional constraints (see Y1GOLD for details). A series of veto masks, including among others masks for bright stars and the Large Magellanic Cloud, reduce the area by $\sim 300 \text{ deg}^2$, leaving $\sim 1500 \text{ deg}^2$ suitable for galaxy clustering study. We explain further cuts to the angular mask in Section IIIB. All data described in this and in subsequent sections are drawn from catalogues and maps generated as part of the DES Y1 Gold sample and are fully described in Y1GOLD.

B. redMaGiC sample

The galaxy sample we use in this work is generated by the REDMAGIC algorithm, run on DES Y1 Gold data. The REDMAGIC algorithm selects Luminous Red Galaxies (LRGs) in such a way that photometric redshift uncertainties are minimized, as is described in [13]. This method is able to achieve redshift uncertainties $\sigma_z/(1 + z) < 0.02$ over the redshift range of interest. The REDMAGIC algorithm produces a redshift prediction $z_{\rm RM}$ and an uncertainty σ_z which is assumed to be Gaussian.

The REDMAGIC algorithm makes use of an empirical red-sequence template generated by the training of the REDMAPPER cluster finder [34, 35]. As described in [35], training of the red-sequence template requires overlapping spectroscopic redshifts, which in this work were obtained from SDSS in the Stripe 82 region [36] and the OzDES spectroscopic survey in the DES deep supernova fields [37].

For the REDMAGIC samples in this work, we make use of two separate versions of the red-sequence training.

-25° -30° 0.30 -35° *n_g* [arcmin⁻² 0.25 -40° DEC -45° 0.20 0.15 -50° 0.10 120° 100° 320° 300 RA

FIG. 1. Galaxy distribution of the REDMAGIC Y1 sample used in this analysis. The fluctuations represent the raw counts, without any of the corrections derived in this analysis. We have restricted the analysis to the contiguous region shown in the figure. The area is 1321 square degrees.



FIG. 2. Redshift distribution of the combined REDMAGIC sample in 5 redshift bins. They are calculated by stacking Gaussian PDFs with mean equal to the REDMAGIC redshift prediction and standard deviation equal to the REDMAGIC redshift error. Each curve is normalized so that the area of each curve matches the number of galaxies in its redshift bin.

The first is based on SExtractor MAG_AUTO quantities from the Y1 coadd catalogs, as applied to REDMAPPER in [38]. The second is based on a simultaneous multi-epoch, multi-band, and multi-object fit (MOF) (see Section 6.3 of Y1GOLD), as applied to REDMAPPER (Mcclintock et al. 2017, in preparation). In general, due to the careful handling of the point-spread function (PSF) and matched

z range	L_{\min}/L_*	$n_{\rm gal} \; ({\rm deg}^{-2})$	$N_{\rm gal}$	Photometry
0.15 < z < 0.3	0.5	0.0134	63719	MAGAUTO
0.3 < z < 0.45	0.5	0.0344	163446	MAGAUTO
0.45 < z < 0.6	0.5	0.0511	240727	MAGAUTO
0.6 < z < 0.75	1.0	0.0303	143524	MOF
0.75 < z < 0.9	1.5	0.0089	42275	MOF

TABLE I. Details of the sample in each redshift bin. $L_{\rm min}/L_*$ describes the minimum luminosity threshold of the sample, $n_{\rm gal}$ is the number of galaxies per square degree, and $N_{\rm gal}$ is the total number of galaxies.

multi-band photometry, the MOF photometry yields lower color scatter and hence smaller scatter in red-sequence photo-zs. For each version of the catalog, photometric redshifts and uncertainties are primarily derived from the fit to the red-sequence template. In addition, an afterburner step is applied to ensure that REDMAGIC photozs and errors are consistent with those derived from the associated REDMAPPER cluster catalog [13].

As described in [13], the REDMAGIC algorithm computes color-cuts necessary to produce a luminositythresholded sample of constant co-moving density. Both the luminosity threshold and desired density are independently configurable, but in practice higher luminosity thresholds require a lower density for good performance. We note that in [13] the co-moving density was computed with the central redshift of each galaxy ($z_{\rm RM}$). For this work, the density was computed by sampling from a Gaussian distribution $z_{\rm RM} \pm \sigma_z$, which creates a more stable distribution near filter transitions. This is



FIG. 3. Correlations of volume-limited REDMAGIC galaxy number density with seeing FWHM and exposure time before any survey property (SP; see text for more details) cuts (illustrated with the red vertical lines) were applied to the mask. In the absence of systematic correlations, the results obtained from these samples are expected to be consistent with no trend (the reference green dashed line). The cuts removed regions with *i*-band FWHM > 4.5 pixels and *i*-band exposure time > 500s as these showed correlations that differed significantly from the mean (> 20%) or were not well fit by a monotonic function. No SP weights were used in this figure.

z range	b^i_{fid}	Δz^i Y1COSMO	Δz^i [Cawthon <i>et al.</i>]
0.15 < z < 0.3	1.45	Gauss $(0.001, 0.008)$	Gauss $(0.008, 0.007)$
0.3 < z < 0.45	1.55	Gauss $(0.001, 0.007)$	Gauss $(-0.005, 0.007)$
0.45 < z < 0.6	1.65	Gauss $(0.003, 0.007)$	Gauss $(0.006, 0.006)$
0.6 < z < 0.75	1.8	Gauss $(0.00, 0.010)$	Gauss $(0.00, 0.010)$
0.75 < z < 0.9	2.0	Gauss $(0.00, 0.010)$	Gauss $(0.00, 0.010)$

TABLE II. Details of the fiducial parameters used for covariance and parameter constraints. Here, $b_{\rm fid}^i$ is the fiducial linear galaxy bias for bin *i* applied to the Gaussian mock surveys we use to construct the covariance matrices. The Δz^i prior is a Gaussian prior applied to the additive redshift bias uncertainty. These were selected to match the analysis in (DES Collaboration *et al.*; Y1COSMO). The lens photo-*z* priors changed somewhat after the Y1COSMO analyses, as described in Cawthon *et al.* 29. We have used the Cawthon *et al.* priors for the galaxy bias measurements presented in Section VI and the abstract, and we used the Y1COSMO priors for the robustness tests in Section VII to be consistent with that analysis. The choice of prior did not impact the results of Y1COSMO or the bias measurements presented here.

the only substantial change to the REDMAGIC algorithm since the publication of [13].

We use REDMAGIC samples split into five redshift bins of width $\Delta z = 0.15$ from z = 0.15 to z = 0.9. We define our footprint such that the data in each redshift bin will be complete to its redshift limit across the entire footprint. To make this possible, we define samples based on a luminosity threshold. Reference luminosities are computed as a function of L_* , computed using a Bruzual and Charlot [39] model for a single star-formation burst at z = 3 [See Section 3.2 35]. Naturally, increasing the luminosity threshold provides a higher redshift sample as well as decreasing the comoving number density. The details of these bins are given in Table I.

In addition to the primary REDMAGIC selection, we also apply a cut on the luminosity $L/L_* < 4$ as this was shown for DES Science Verification to reduce the stellar contamination in the sample, although this is mostly superfluous for Y1 Gold. During testing, we find that the observational systematic relationships for the $0.5L_*$ sample, used for z < 0.6, are minimized for the MAG_AUTO sample, with a very minor impact on photo-z performance. For $L_* \geq 1.0$, used for z > 0.6, we instead find that the observation systematic relationships are minimized for the MOF sample, and that the photo-z performance is also improved. Consequently, we use MAG_AUTO for our z < 0.6 sample and MOF for z > 0.6. See Section V for further discussion.

We build the area mask for the REDMAGIC samples based on the depth information produced with the RED-MAGIC catalogs. This information is provided by the $z_{\rm max}$ quantity, which describes the highest redshift at which a typical red galaxy of the adopted luminosity threshold (e.g. $0.5L_*$) can be detected at 10σ in the z-band, at 5σ in the r and i-bands, and at 3σ in the gband, as described in Section 3.4 of [35]. The quantity $z_{\rm max}$ varies from point to point in the survey due to observing conditions. Consequently, we construct a z_{\max} map, specified on a HEALPIX map with $N_{\rm side} = 4096$. In order to obtain a uniform expected number density of galaxies across the footprint, we only use regions for which $z_{\rm max}$ is higher than the upper edge of the redshift bin under consideration. The footprint is defined as the regions where this condition is met in all redshift bins. Thus, we only use pixels that satisfy each of the conditions where the $0.5L_*$ sample is complete to z = 0.6, the

 $1.0L_*$ sample is complete to z = 0.75, and the $1.5L_*$ sample is complete to z = 0.9. We also restrict the analysis to the contiguous region shown in Figure 1.

An additional 1.6% of the footprint is vetoed because it has extreme observing conditions. The selection of these cuts is detailed in Section V.

After masking and additional cuts, we obtain a total sample of 653,691 objects distributed over an area of 1321 square degrees, as shown in Fig. 1. The average redshift uncertainty of the sample is $\sigma_z/(1 + z) = 0.0166$. The redshift distribution of each bin can be seen in Figure 2. The number of objects in each bin increases up to z = 0.6 due to the increase in volume, and decreases at higher redshift due to the increased luminosity threshold.

IV. ANALYSIS METHODS

A. Clustering estimators

We measure the correlation functions $w(\theta)$ using the Landy & Szalay estimator [40]

$$\hat{w}(\theta) = \frac{DD - 2DR + RR}{RR} \,, \tag{4}$$

where DD, RR and DR are the number of pairs of galaxies from the galaxy sample D and a random catalog R. This is calculated in 20 logarithmically separated bins in angle θ between 2.5 arcmin and 250 arcmin to match the analysis in Y1COSMO. We use 60 times more randoms than data. The pair-counting was done with the package tree-corr [41] available at https://github.com/rmjarvis/TreeCorr.

We also calculate cross-correlations between the galaxy sample and a suite of potential contaminants, including observational conditions and survey property maps, described in Sec. V. As these properties are best described in pixelated map format, for these cross-correlations we use a pixel-based estimator. Using the notation of [17], the correlation between two maps N_1 and N_2 of mean values \bar{N}_1, \bar{N}_2 is estimated as

$$\hat{w}_{1,2}(\theta) = \sum_{i=1}^{N_{\text{pix}}} \sum_{j=i}^{N_{\text{pix}}} \frac{(N_{i,1} - \bar{N}_1)(N_{j,2} - \bar{N}_2)}{\bar{N}_1 \bar{N}_2} \Theta_{i,j}, \quad (5)$$

where the sum runs through all pairs of the N_{pix} pixels in the footprint, $N_{i,1}$ is the value of the N_1 map in pixel i, and $\Theta_{i,j}$ is unity when the pixels i and j are separated by an angle θ within the bin size $\Delta \theta$.

B. Covariances

The fiducial covariance matrix we use for the $w(\theta)$ measurement is a theoretical halo model covariance, described and tested by [20]. This same covariance is used for Y1COSMO.

For the analysis of observational systematics and their correlation with the data, we use a set of 1000 mock survevs (hereafter 'mocks') based on Gaussian random field realizations of the projected density field. These are then used to obtain an alternative covariance, which includes all the mask effects as in the real data. The mocks we use were produced using the following method. We first calculate, using CAMB [24], the galaxy clustering power spectrum $C_i^{gg}(\ell)$, assuming the fiducial cosmology with fixed galaxy bias b^i for each redshift bin *i*; the galaxy bias values are listed in Table II. The angular power spectrum is then used to produce a full-sky Gaussian random field of δ_q . We apply a mask to this field corresponding to the Y1 data, as shown in Fig. 1. This is converted into a galaxy number count N_{gal} as a function of sky position, with the same mean as the observed number count \bar{N}_o in each redshift bin, using

$$N_{\rm gal} = N_o (1 + \delta_g). \tag{6}$$

Shot noise is finally added to this field by Poisson sampling the $N_{\rm gal}$ field.

In order to avoid pixels with $\delta_g < -1$, which cannot be Poisson sampled, we follow the method used by [20]: before Poisson sampling, we multiply the density field by a factor α , where $\alpha < 1$; we then rescale the number density $n_{\rm gal}$ by $1/\alpha^2$ in order to preserve the ratio of shotnoise to sample variance; we then rescale the measured $w(\theta)$ by $1/\alpha^2$ to obtain the unbiased $w(\theta)$ for each mock. This procedure is summarized by

$$\delta_g \to \alpha \delta_g \,, \tag{7}$$

$$n_{\rm gal} \rightarrow n_{\rm gal}/\alpha^2$$
, (8)

$$w(\theta) \rightarrow w(\theta)/\alpha^2$$
. (9)

We then use these mocks to estimate statistical errors in galaxy number density as a function of potential systematics. Alternatively we "contaminate" each of the 1000 mocks with survey properties as discussed in Section V to assess the impact of systematics on the $w(\theta)$ covariance. Note that these mocks would not be fully realistic for $w(\theta)$ covariance and cosmological inference as they are basically Gaussian realizations. These mocks allow us to quantify significances (i.e., a $\Delta \chi^2$) to null tests, which are a necessary step in our analysis. Further, given such a large number of realizations we are able to obtain estimates of both the impact of the systematic correction on the resulting statistical uncertainty and any bias imparted by our methodology to well below 1σ significance (e.g., given 1000 mocks, a 0.1σ bias can be detected at 3σ significance).

V. SYSTEMATICS

A. Survey property (SP) maps

The number density of galaxies selected based on their imaging is likely to fluctuate with the imaging quality



FIG. 4. Galaxy number density divided by the mean number density across the footprint for each redshift bin, split by the number density of stars. The points with error-bars display the results for our $3\Delta\chi^2(68)$ weighted sample, the cyan curves display the results without these weights. For the weighted sample, the χ^2 of $N_{\rm gal}/\langle N_{\rm gal}\rangle = 1$ for each bin is 24.9, 16.0, 13.1, 6.6 and 10.9, and the $\Delta\chi^2$ is 0.99, 0.95, 0.24, 0.013, and 0.082 with $N_{\rm d.o.f} = 10$. We see no evidence for stellar contamination or obscuration in this sample.



FIG. 5. Galaxy number density in the highest redshift bin, 0.75 < z < 0.9, as a function of two example SP maps, FWHM *r*-band and FWHM *i*-band. The black points correspond to the $3\Delta\chi^2(68)$ weighted sample, the cyan line is the unweighted sample. In this redshift bin, the SP maps used in the $3\Delta\chi^2(68)$ weights were Airmass *i* and FWHM *r*. The left panel demonstrates the effect of the weights on the FWHM *r* correlation. The right panel demonstrates that correlations with SP maps that were not included in the weights are still reduced due to correlations among the SP maps. The full set of SP correlations for the maps in Table III are shown in Appendix A.

due to fluctuations in the noise (e.g., Malmquist bias) and limitations in the reduction pipeline. Such fluctuations can imprint the structure of certain survey properties onto the galaxy field, thereby producing a noncosmological signal. In order to quantify the extent of these correlations and remove their effect from the twopoint function, maps of DES imaging properties were produced using the methods described in Ref. [42]. We consider the possibility that depth, seeing, exposure time, sky brightness and airmass, in each band griz, affect the density of galaxies we select.

In total, we consider 21 survey property maps. We refer to these as SP maps from here on:

- depth: the magnitude limit at which we expect to be able to detect a galaxy to 10σ significance;
- seeing FWHM: the full width at half maximum of the PSF of a point source;
- exposure time: total exposure time in a given band;
- sky brightness: the brightness of the sky, e.g., due to background light or the Moon phase;

• airmass: the amount of atmosphere a source has passed through, normalized to be 1 when pointing at zenith.

Where relevant, we use the weighted average quantity over all exposures contributing to a given area.

We also consider Galactic extinction and stellar contamination (or obscuration [14]) as potential systematics. The stellar density map was created by selecting moderately bright, high confidence stars. Using the notation of Y1GOLD, this selection is $MODEST_CLASS = 2$ with 18.0 < i < 20.5, FLAGS_GOLD = 0, and BADMASK ≤ 2 . We also include an additional color cut of 0.0 < q - i < 3.5and g - r > 0. These stars were binned in pixels with $N_{\rm side} = 512$ (equivalent to 47 square arcmin), and the corresponding area for each pixel was computed at higher resolution $(N_{\text{side}} = 4096)$ from the Y1 Gold footprint and pixel coverage fraction, as well as the bad region mask. Together, this yields the number of moderately bright stars per square degree that can be used to cross-correlate galaxies with stellar density. Using MODEST_CLASS to select stars means this map could potentially contain DES galaxies. For this reason, we test for correlations with

the astrophysical maps separately to the SP maps. As we find no correlation between stellar density and galaxy density, we do not take this contamination into account. For Galactic extinction, we use the standard map from [43].

B. Systematic corrections

This section describes the method used to identify and correct for observational systematics. We also discuss the uncertainty on this correction and its impact on the $w(\theta)$ covariance. Our approach is to first identify maps that are correlated with fluctuations in the galaxy density field at a given significance. We then correct for the contamination using weights to be applied to the galaxy catalog.

As demonstrated by [44], when testing a large number of maps one expects there to be some amount of covariance between the maps and the true galaxy density field due to chance. Consequently, it is possible to over-correct the galaxy density field using the type of methods employed in this work. To limit this effect, we do not correct for all possible maps, and limit ourselves to those maps that are detected to be correlated with the galaxy density field at high significance (above a given threshold). We test the robustness of the results on our choice of threshold in Section VIIA and we test for biases due to over-correction in Section VIIC. The end result of our procedure is a measurement of $w(\theta)$ that is free of systematics above a given significance (in our concrete case a galaxy density free of two sigma correlations with SP maps, as defined below, and visualized in Fig. III) and that can be directly utilized in combination with weak lensing measurements for cosmological analyses.

We identify the most significant SP maps as follows. First, given an SP map of some quantity s, we identify all pixels in some bin $s \in [s_{\min}, s_{\max}]$. We then compute the average density of galaxies in these pixels. By scanning across the whole range of possible *s*-values for the SP map, we can directly observe how the galaxy density field scales with *s*. Examples of these type of analyses are shown in Figs. 3, 4 and 5.

We first remove regions of the footprint that display either especially significant (> 20%) changes in galaxy density from the mean, or are poorly fit by a monotonic function. These regions are defined from the cuts shown in Fig 3. We remove regions of the footprint with *i*-band FWHM > 4.5 and *i*-band exposure time > 500s. These cuts remove 1.6% of the Y1 area.

After cutting the footprint, we determine which SP maps most significantly correlate with the data by fitting a linear function to each number density relationship. We minimize a $\chi^2_{\rm model}$ where the model is $N_{\rm gal} \propto A \, s + B$. We determine the significance of a correlation based on the difference in χ^2 between the best-fit linear parameters,

z range	Maps included in	Maps included in
0	$3\Delta\chi^2(68)$ weights	$2\Delta\chi^2(68)$ weights
0.15 < z < 0.3	Depth (r)	Exptime (i)
		FHWM (z)
		FWHM (r)
		Airmass (z)
0.3 < z < 0.45	Depth (g)	Depth (g)
0.45 < z < 0.6	FWHM (z)	FWHM (z)
	Exptime (g)	Exptime (g)
	FWHM (r)	FWHM (r)
	Skybright (z)	Skybright (z)
		Depth (i)
0.6 < z < 0.75	FWHM (gri) PCA-0	FWHM (gri) PCA-0
	Skybright (r)	Skybright (r)
	FWHM (z)	FWHM (z)
		Exptime (i)
		Exptime (z)
0.75 < z < 0.9	Airmass (i)	Airmass (i)
	FWHM (r)	FWHM (r)
	·	FWHM (g)

TABLE III. List of the maps used in the SP weights. Each of these has been determined to impart fluctuations in our galaxy sample at > $3\Delta\chi^2(68)$ or > $2\Delta\chi^2(68)$ significance. The weights were applied serially for each map in the order shown, starting from the top of the table. 'FWHM' refers to the full-width-half-maximum size of the PSF. The photometric band of each SP map is in parentheses.

and a null test of $N_{\rm gal}/\langle N_{\rm gal}\rangle = 1$,

$$\Delta \chi^2 = \chi^2_{\text{null}} - \chi^2_{\text{model}} \,. \tag{10}$$

The $\Delta \chi^2$ is then compared to the same quantity measured on the Gaussian random fields described in Section IV B. We then label each potential systematic to be significant at 1σ if the $\Delta \chi^2$ measured on the data is larger than 68% of the mocks respectively. We denote this threshold as $\Delta \chi^2(68)$ and quote significances as $\Delta \chi^2 / \Delta \chi^2(68)$; the square-root of this number should roughly correspond to the significance in terms of σ . Some examples of these tests for the observational systematics can be seen in Fig. 6. The full set of tests can be seen in Appendix A. We see no significant correlation with stellar density in the sample, as shown in Fig. 4. Similarly, we find no correlations with Galactic extinction. Thus, our main tests are against SP maps, which are particular to DES observations.

Once we identify the most significant contaminant SP maps, we define weights to be applied to the galaxy sample in order to remove the dependency, following a method close to that of the latest LSS survey analysis [5, 45, 46]. Note however that we identify systematics using a rigorous χ^2 threshold significance criteria, based on a large set of Gaussian realizations, which to our knowledge was not done before.

For this method we apply the following steps to each redshift bin separately. The correlation with a systematic s is fitted with a function $N_{\text{gal}}/\langle N_{\text{gal}}\rangle = F_{\text{sys}}(s)$.



FIG. 6. The significance of each systematic correlation. The significance is calculated by comparing the $\Delta \chi^2$ measured on the data to the distribution in the mock realizations. We find the 68th percentile $\Delta \chi^2$ value, labeling it $\Delta \chi^2$ (68), for each map obtained from the mock realizations. We quote the significance for the relationship obtained on the data as $\Delta \chi^2 / \Delta \chi^2$ (68). Weights are applied for the SP map with the largest significance, with the caveat that we do not correct for both depth and the components of depth (e.g. exposure time, PSF FWHM) in the same band. For example, in the bin 0.15 < z < 0.3, correcting for *r*-band depth (the most significant contaminant) did not remove all the *r*-band correlations with $\Delta \chi^2 / \Delta \chi^2$ (68) > 2, so is not included in the final $2\Delta \chi^2 / \Delta \chi^2$ (68) and $3\Delta \chi^2 / \Delta \chi^2$ (68). The *x* axis is shown in order of decreasing significance for the unweighted sample. The labels in **bold** are the SP maps included in the $2\Delta \chi^2 / \Delta \chi^2$ (68) weights are the same because correcting for only *g*-band depth removes all correlations with $\Delta \chi^2 / \Delta \chi^2$ (68) and $2\Delta \chi^2 / \Delta \chi^2$ (68) weights are the same because correcting for only *g*-band depth removes all correlations with $\Delta \chi^2 / \Delta \chi^2$ (68) > 2.

For depth and airmass, the function used was a linear fit in s. For exposure time and sky brightness, the function was linear in \sqrt{s} , as this is how these quantities enter the depth map. For the seeing correlations, we fit the model

$$N_{\rm gal}/\langle N_{\rm gal} \rangle = F_{\rm sys} \left(s_{\rm FWHM} \right)$$
$$F_{\rm sys} \left(s_{\rm FWHM} \right) = A \left[1 - \operatorname{erf} \left(\frac{s_{\rm FWHM} - B}{\sigma} \right) \right], (11)$$

where $s_{\rm FWHM}$ is the seeing full-width half-max value, and A, B and σ are parameters to be fitted. This functional



FIG. 7. Two-point correlation functions for the fiducial analysis in each combination of the 5 redshift bins. The left panel shows the auto-correlation used in Y1COSMO and the galaxy bias measurements. A correction for correlations with survey properties is applied according to the methodology in Section V. The grey dashed line is the correlation function calculated without the SP weights. The black points use the $2\Delta\chi^2(68)$ weights. The right panel shows the cross-correlation of the redshift bins, shown here as a consistency check. These measurements are expected to be non-zero, with a significance related to the degree of overlap in the n(z) displayed in Fig. 2. The numbers in each panel correspond to the redshift bins used in the crosscorrelation. The error-bars in the cross-correlations were calculated using the log-normal mock surveys used for Y1COSMO covariance validation [20]. We show correlations down to $\theta = 10'$ to highlight the goodness of the fit towards small scales, but data points within grey shaded regions have not been used in bias constraints or the galaxy clustering part of Y1COSMO. That scale cut has been set in co-moving coordinates at $8 \text{ Mpc } h^{-1}$. The solid red curve is the best-fit model using only the $w(\theta)$ auto-correlations at fixed cosmology, using Δz^i priors from [29]. The solid blue curve is the best-fit model from the full cosmological analysis in Y1COSMO. For many of the cross-correlation panels, these predictions are indistinguishable.

form matches that applied to BOSS [46, 47]; we believe it is thus the expected form when morphological cuts are applied to reject stars (as this is what causes the relationship for BOSS).

Each galaxy i in the sample is then assigned a weight $1/F_{\rm sys}(s_i)$ where s_i is the value of the systematic at the galaxy's location on the sky. This weight is then used when calculating $w(\theta)$ and in all further null tests.

In this sample we find evidence of multiple systematics at a significance of $\Delta \chi^2 / \Delta \chi^2(68) > 3$, some of which are correlated with each other. To account for this, we first apply weights for the systematic with the highest $\Delta \chi^2 / \Delta \chi^2(68)$. Then, using the weighted sample, we remeasure the significance of each remaining potential systematic and repeat the process until there are no systematics with a significance greater than a $\Delta\chi^2/\Delta\chi^2(68) = 3$ threshold. The final weights are the product of the weights from each required systematic. We also produce weights using a threshold of $\Delta\chi^2/\Delta\chi^2(68) = 2$, allowing us to determine if using a greater threshold has any impact on our clustering measurements. We refer to these weights as the $3\Delta\chi^2(68)$ and $2\Delta\chi^2(68)$ weights respectively.

The final weights used in this sample are described in Table III. The SP maps are either the depth or properties that contribute to the depth (e.g. holding everything else fixed, a longer exposure time will result in an increased depth). Thus, in bins where multiple SP weights were

z range	b^i	r^i
0.15 < z < 0.3	1.40 ± 0.077	1.09 ± 0.07
0.3 < z < 0.45	1.61 ± 0.051	0.97 ± 0.06
0.45 < z < 0.6	1.60 ± 0.040	0.93 ± 0.08
0.6 < z < 0.75	1.93 ± 0.045	1.02 ± 0.13
0.75 < z < 0.9	1.99 ± 0.066	0.96 ± 0.28

TABLE IV. The measurements of galaxy bias b^i and the ratio of bias from clustering and galaxy-galaxy lensing r^i for each redshift bin *i*, calculated with cosmological parameters fixed at the mean of the Y1COSMO posterior, varying only bias and nuisance parameters with lens photo-*z* priors from [29].

required, we avoided correcting for both depth and SPs that contribute to the depth in the same band. In these cases, we weight for only the SPs that contribute to the depth. Fig. A.2 shows the correlation between the sample density and the SP maps used in Table III, both with and without weights.

Fig. 6 summarizes the results of our search for contaminating SPs, for each redshift bin. The blue points show the significance for each map, prior to the application of any weights. The black and red points display the significance after applying the $3\Delta\chi^2(68)$ and $2\Delta\chi^2(68)$ weights respectively. In Section VII, we will test our results with both choice of weights and whether to expect any bias from over-correction from either choice.

When $F_{\text{sys}}(s)$ is a linear function, the method described above, hereby referred to as the weights method, should be equivalent to the method used in [15, 17]. This has been shown in [5] for the DES science verification redMaGiC sample.

The impact of the SP weights on the $w(\theta)$ measurement can be seen in Figure 7. The dashed line displays the measurement with no weights applied. One can see that in all redshift bins, the application of the SP weights reduces the clustering amplitude and that the effect is greatest on large scales. This is consistent with expectations (see, e.g. Ref. [14]).

VI. RESULTS: GALAXY BIAS AND STOCHASTICITY

The $w(\theta)$ auto- and cross-correlation functions of the REDMAGIC galaxy sample are shown in Figure 7. We show the auto-correlation calculated with and without a correction for observational systematics, as described in Sec V. A minimum angular scale θ_{\min}^i has been applied to each redshift bin *i*. These were chosen to be $\theta_{\min}^1 = 43'$, $\theta_{\min}^2 = 27'$, $\theta_{\min}^3 = 20'$, $\theta_{\min}^4 = 16'$, and $\theta_{\min}^5 = 14'$ to match the analysis in Y1COSMO. These minimum angular scales, varying with redshift, correspond to a single minimum co-moving scale $R = 8 \,\mathrm{Mpch}^{-1}$ such that $\theta_{\min}^i = R/\chi(\langle z^i \rangle)$, where $\langle z^i \rangle$ is the mean redshift of galaxies in bin *i* [20].

The angular correlation function has been calculated

on scales below θ_{\min}^i , but these were removed in all parameter constraints.

Fixing all cosmological parameters, including Ω_m , at the Y1COSMO values, we measure the linear bias to be $b_1 = 1.40 \pm 0.08$, $b_2 = 1.61 \pm 0.050$, $b_3 = 1.60 \pm 0.040$, $b_4 = 1.93 \pm 0.05$, and $b_5 = 1.99 \pm 0.07$. The combined goodness-of-fit χ^2 of these measurements is $\chi^2 = 76$ for 52 data points. This was calculated using only the auto-correlations.

For the $L/L_* > 0.5$ sample, the bias is nearly constant as a function of redshift, though there is a decrease at low redshift that has more than 2σ significance (the correlation in the measured bias for bins 1 and 3 is only -0.04, so we can safely ignore it in this discussion). The decrease is less significant if we determine the expectation for a passively evolving sample as in [48, 49], which predicts a bias of 1.52 at z = 0.24 given a bias of 1.61 at z = 0.53. The bias increases for the higher luminosity sample, as expected. The results are broadly consistent with previous studies of the bias of red galaxies at low redshift (see, e.g., [50] for a review) and BOSS at intermediate redshifts (see, e.g., [51]). Further study of the details of the REDMAGIC samples is warranted, especially if one wishes to use $w(\theta)$ at scales smaller than those studied in Y1COSMO.

In the right panel of Figure 7, we present the crosscorrelation measurement of REDMAGIC galaxies in different redshift bins. For the cross-correlation, we use a covariance matrix calculated from log-normal simulations described in [20]; the square root of the diagonal of this covariance matrix yields the error-bars shown in the figure. These are the same simulations used to validate the Y1COSMO covariance matrix. We overplot the cross-correlation prediction both from the best fit bias values from the auto-correlations, and the best fit cosmology and bias from Y1COSMO. This figure is intended to give the reader a sense of the magnitude of the measured cross-correlations and not as a robustness test, hence we do not include a goodness-of-fit for this measurement.

We compare these bias constraints to those measured from the galaxy-galaxy lensing probe of the same RED-MAGIC sample, presented in Y1GGL. We parameterize the difference between the two measurements with the cross-correlation coefficients r^i , which are presented in Figure 8. Beyond linear galaxy bias, r can deviate from 1 and acquire scale dependences, and it must be properly modeled to constrain cosmology with combined galaxy clustering and galaxy-galaxy lensing (e.g. [52]). With our choice of scale cuts, we see no evidence of tension between the two bias measurements. This provides further justification for fixing r = 1 in the Y1COSMO analysis.

VII. DEMONSTRATION OF ROBUSTNESS

We apply a number of null tests to our weighted sample to demonstrate its robustness. We do so by obtaining constraints on the galaxy bias and Ω_m . These parameters



FIG. 8. Constraints on the ratio, r, of galaxy bias measured on $w(\theta)$ and measured from the galaxy-galaxy lensing signal (see [30] denoted Y1GGL in the text) in each redshift bin (first five panels from left to right, top to bottom). The bottom-right panel then displays the individual measurements for each bin (purple for our $w(\theta)$ measurements and orange for those obtained in Y1GGL). All cosmological parameters were fixed at the DES Y1COSMO posterior mean values, using Δz^i priors from [29]. The constraints were calculated using the full Y1COSMO covariance matrix, so the covariance between the two probes has been taken into account. We see no significant evidence for $r \neq 1$ within the errors.

are sensitive to both multiplicative and additive shifts in the amplitude of $w(\theta)$ and we therefore believe they should encapsulate any potential systematic bias that could affect the cosmological analysis of Y1COSMO. We thus perform joint fits to the data in each redshift bin to obtain constraints on the five b^i and Ω_m . For these fits, we marginalize over an additive redshift bias uncertainty described in Table II. All other cosmological parameters are fixed at the Y1COSMO cosmology and as such, this should not be interpreted as a true measurement of Ω_m . Results are obtained using the analysis pipeline described in [20]. We describe how $w(\theta)$ is altered to perform each test throughout the rest of this section.

A. Selection of threshold

We test two thresholds used to determine determine when to apply weights based on a given SP map: $3\Delta\chi^2(68)$ and a more restrictive (i.e., more maps weighted for) $2\Delta\chi^2(68)$. After reaching a certain thresh-

old, we expect that the only effect from adding extra weights would be to bias the measurements (from overcorrection) and add greater uncertainty. We test for those effects in the following subsections. Here, in order to demonstrate that our results are insensitive to the choice in threshold, the change in the measured b^i and Ω_m must be negligible compared to its uncertainty.

Figure 9 shows the difference between the $3\Delta\chi^2(68)$ and $2\Delta\chi^2(68)$ SP weights. Because the weights correction can only decrease the $w(\theta)$ signal, applying a stricter threshold significance is expected to move the contours towards smaller values of b^i . Figure 9 shows that this impact is very small compared to the overall Y1 uncertainty and we can conclude that the choice between $3\Delta\chi^2(68)$ and $2\Delta\chi^2(68)$ weights will have negligible impact on the Y1COSMO parameter constraints (The final weights used in Y1COSMO are the $2\Delta\chi^2(68)$ weights).

Figure 9 also shows the impact of not including SP weights on the parameter constraints. Ignoring the SP correlations would have resulted in significantly bias constraints on b^i and Ω_m . In every redshift bin, the shift is



FIG. 9. Parameter constraints showing the impact of the SP weights, varying Ω_m , 5 linear bias parameters b^i , and 5 nuisance parameters Δz^i . Contours are drawn at 68% and 95% confidence level. These constraints use the same Δz^i priors as Y1COSMO. The blue contour shows the constraints on $w(\theta)$ calculated with no SP weights. The gray and red contours use SP weights removing all $2\Delta\chi^2(68)$ and $3\Delta\chi^2(68)$ correlations respectively. In this parameter space, ignoring the correlations with survey properties would have significantly biased the constraints from $w(\theta)$. As expected, the best fit when using the $2\Delta\chi^2(68)$ weights is at smaller values of b^i than the $3\Delta\chi^2(68)$ weights, although the difference is not significant compared to the size of the contour.

greater than 2σ along the major axis of the ellipses.

the bias in $w(\theta)$ to be,

B. Estimator bias

We also test for potential bias in $w(\theta)$ induced by overcorrecting with the weights method and from correlations between the SP maps. This was done using the Gaussian mocks described in Section IV B using the following method. After the galaxy over-density field has been generated in each realization, we insert the systematic correlation using $F_{sys}(s)$ and the best-fit parameters for each of the systematics in Table III at $2\Delta\chi^2(68)$ significance. This is equivalent to dividing each mock galaxy map by a map of the SP weights.

We then produced a galaxy number count as before, also adding shot noise. We fit the parameters of $F_{\rm sys}(s)$ to each realization and apply weights to the maps using the same method that is applied to the data. We measure $w(\theta)$ using the pixel estimator in Eqn. 5 on mocks with systematic contamination and correction, $w_{\rm weights}$, and on mocks with no systematics added, $w_{\rm no \ sys}$. We define

$$w_{\text{est bias}} = \frac{1}{N} \left(\sum_{i=1}^{N} w_{\text{no sys},i} - \sum_{j=1}^{N} w_{\text{weights},j} \right)$$
(12)

where N is the total number of realizations. We then add $w_{\text{est bias}}$ to the measured $w(\theta)$ and measure b^i and Ω_m . This test is designed to test for any bias in $w(\theta)$ induced by the the estimator when using weights.

This result can be seen in Figure 10 where it shows negligible impact on the parameter constraints.

C. False correlations

Given the large number of SP maps being used in the systematics tests, it is possible that chance correlations will appear significant and weights will be applied where no contamination has occurred, biasing the measured signal. To test this, we use the same Gaussian mocks as in



FIG. 10. Parameter constraints showing the impact of the estimator bias, w_{est} and false correction bias w_{false} . The fiducial data vector and was calculated using the $2\Delta\chi^2(68)$ weights on the data. The w_{est} and w_{false} were measured on Gaussian mock surveys using a $2\Delta\chi^2(68)$ threshold significance. We see no evidence for significant bias in the b^i , Ω_m plane. These constraints use the same Δz^i priors as Y1COSMO.

Section VIIB with no added systematic contaminations. We measure the correlation of each mock with each of the 21 SP maps in Section VA, identifying any correlations above a $2\Delta\chi^2(68)$ threshold significance.

The false correction bias $w_{\text{false bias}}$, is then defined as the average difference between the $w(\theta)$ measured with no corrections, and the $w(\theta)$ measured correcting for all correlations above the threshold using the weights method. We then add $w_{\text{false bias}}$ to the measured $w(\theta)$ and test the impact on b^i and Ω_m constraints.

This test is designed to test for any bias in $w(\theta)$ induced by falsely correcting for SP maps that where only correlated with the galaxy density by chance.

This result is shown in Figure 10 where $w_{\text{false bias}}$ for the $2\Delta\chi^2(68)$ SP maps has been used. This shows a negligible impact on the constraints. The $w_{\text{false bias}}$ for the $3\Delta\chi^2(68)$ SP maps is not shown as it has an even smaller impact. This demonstrates that selecting a $2\Delta\chi^2(68)$ threshold does not induce a bias in the inferred bias parameters for the set of SP maps used in this analysis.

D. Impact on covariance

Correcting for multiple systematic correlations can alter the covariance of the $w(\theta)$ measurement in various ways. We expect that scatter in the best fit parameters should increase the variance, while the removal of some clustering modes should decrease it. We test the significance of any any changes to the amplitude and structure of the covariance matrix using the Gaussian mocks.

For this test we use the same mocks as in Section VII B which are 'contaminated' with the same systematic correlations found in the data. We fit the $F_{\rm sys}(s)$ function to each mock and correct using weights. We then measure the correlation function $w_{\rm weights}$ and calculate the covariance matrix of this measurement. We also measure the correlation on mocks with no systematics added, $w_{\rm no\ sys}$, and calculate the covariance matrix from each measurement. We calculate the galaxy bias b^i and Ω_m constraints for each covariance matrix and test if the resulting contours are significantly different. This test determines whether this additional uncertainty needs to be considered in the Y1COSMO analysis by marginalizing over the fitted parameters.

The results of this test are shown in Figure 11. We show that for the SP maps selected in this analysis, the



FIG. 11. Parameter constraints showing the impact of the systematics correction on the covariance. Both contours use the fiducial theory data vector. The blue contour uses the covariance from mock surveys with no contamination added (labeled "cov: no sys"). The gray contour uses the covariance determined from mock surveys with the $2\Delta\chi^2(68)$ contaminations added (labeled "cov: 2σ sys"). These constraints use the same Δz^i priors as Y1COSMO.

impact on the size of the contours is negligible. We have therefore not included any additional parameters in the MCMC analysis to account for the uncertainty in the correction.

VIII. CONCLUSIONS

We have presented the 2-point angular galaxy correlation functions, $w(\theta)$, for a sample of luminous red galaxies in DES Y1 data, selected by the REDMAGIC algorithm. This yielded a sample with small redshift uncertainty, a wide redshift range, and wide angular area. We split this sample into five redshift bins and analyzed its clustering. Our findings can be summarized as follows:

• We find that multiple systematic dependencies between REDMAGIC galaxy density and survey properties must be corrected for in order to obtain unbiased clustering measurements. We correct for these dependencies by adding weights to the galaxies, following [45, 46].

• We demonstrate both that our methods sufficiently remove systematic contamination (no significant differences are found between applying a $2\Delta\chi^2(68)$ and $3\Delta\chi^2(68)$ threshold; see Fig. 9) and that any bias resulting from our method removing true clustering modes is insignificant (see Fig. 10). We further demonstrate that our weighting method imparts negligible changes to the covariance matrix (see Fig. 11).

• We find the redshift and luminosity dependence of the bias of REDMAGIC galaxies to be broadly consistent with expectations for red galaxies.

• We find that the large-scale galaxy bias is consistent with that determined by the Y1GGL galaxy-galaxy lensing measurements. This is consistent with r = 1 at linear scales, in agreement with basic galaxy formation theory, and a key assumption in the Y1COSMO analysis. (See Fig. 8.)

• Our results give an unbiased $w(\theta)$ data vector to be provided to the Y1COSMO analysis, thereby yielding direct measurements of the amplitude of matter clustering with unprecedented precision.

The methods we have presented, both correcting for systematic dependencies and ensuring the robustness of these corrections, can be used as a guide for future analyses. Possible improvements to the work include incorporating image simulations [53] and using mode projection techniques [16].

Our galaxy bias results can be extended to study luminosity dependence within redshift bins and to use smaller scale clustering in order to determine the HOD of RED- MAGIC galaxies. Already, our bias measurements can be used to inform simulations (e.g., for the support of DES Y3 analyses) and additional HOD information would be of further benefit.

Finally, the results presented here have been optimized for combination with other cosmological probes in Y1COSMO and our work has ensured the galaxy clustering measurements do not bias the Y1COSMO results. The analysis followed a strict blinding procedure and has yielded unprecedentedly precise and robust constraints when combined with the other 2-point functions.

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Appendix A: Survey Property Maps

In this appendix we present some examples of the survey property maps used throughout the analysis. These can be seen in Fig A.1.

In Fig A.2 we show the correlations between the galaxy density and all the SP maps listed in Table III.



FIG. A.1. Maps of potential sources of systematics. Shown here for *i*-band only. Maps in other bands show fluctuations on similar scales. Each SP map is shown at $N_{\text{side}} = 1024$. The stellar density map is shown at $N_{\text{side}} = 512$.



FIG. A.2. Galaxy number density as a function of different SP maps. We show here only the correlations with SP maps used in the $2\Delta\chi^2(68)$ weights calculation. The cyan line is the correlation of the sample without weights. The black points show the correlation after correction with the $2\Delta\chi^2(68)$ weights. The error bars were calculated by measuring the same correlation on the Gaussian mock surveys described in Section IV B. The significance of these correlations are shown in Figure 6.