Dark Energy Survey Year 1 Results: Galaxy Sample for BAO Measurement

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ABSTRACT

We define and characterise a sample of 1.3 million galaxies extracted from the first year of Dark Energy Survey data, optimised to measure Baryon Acoustic Oscillations in the presence of significant redshift uncertainties. The sample is dominated by luminous red galaxies located at redshifts $z \gtrsim 0.6$. We define the exact selection using color and magnitude cuts that balance the need of high number densities and small photometric redshift uncertainties, using the corresponding forecasted BAO distance error as a figure-of-merit in the process. The typical photo-z uncertainty varies from 2.3% to 3.6% (in units of 1+z) from z = 0.6 to 1, with number densities from 200 to 130 galaxies per deg² in tomographic bins of width $\Delta z = 0.1$. Next we summarise the validation of the photometric redshift estimation. We characterise and mitigate observational systematics including stellar contamination, and show that the clustering on large scales is robust in front of those contaminants. We show that the clustering signal in the auto-correlations and cross-correlations is generally consistent with theoretical models, which serves as an additional test of the redshift distributions.

Key words: cosmology: observations - (cosmology:) large-scale structure of Universe

1 INTRODUCTION

The use of the imprint of Baryon Acoustic Oscillations (BAO) in the spatial distribution of galaxies as a standard ruler has become one of the common methods in current observational cosmology to understand the Universe. The physics that causes BAO is well understood. Primordial perturbations generated acoustic waves in the photon-baryon fluid until decoupling $(z \sim 1100)$. These sound waves lead to the large oscillations observed in the power spectrum of the CMB anisotropies, but they are also visible in the clustering of matter, and therefore galaxies, as a high density region around the original source of the perturbation, at a distance given by the sound horizon length at recombination. This high density region shows as a small excess in the number of pairs of galaxies separated by ~ 150 Mpc. Since the sound horizon is very precisely measured in the cosmic microwave background (Planck Collaboration et al. 2016), the BAO measurements can be used as a standard ruler. This is, therefore, a geometrical probe of the expansion rate of the Universe, that maps the angular diameter distance and the Hubble parameter as functions of the redshift. There have now been multiple detections of the BAO in redshift surveys (Eisenstein et al. 2005; Percival et al. 2010; Ross et al. 2015; Alam et al. 2017; Ata et al. 2018; Delubac et al. 2015; Bautista et al. 2017; Percival et al. 2001; Cole et al. 2005; Blake et al. 2011; Beutler et al. 2011) and it is considered as one of the main cosmological probes for current and planned cosmological projects.

A key feature of the BAO method is the fact that the sound horizon length is large, and, therefore, very deep and wide galaxy surveys are needed in order to reach precise measurements of the BAO scale. But, at the same time, this large scale protects the BAO feature from large corrections due to astrophysical and non-linear effects of structure formation and therefore from systematic errors, making BAO a solid probe of the expansion rate of the Universe.

The Dark Energy Survey (DES) is one of the most important of the currently ongoing large galaxy surveys and, as its name suggests, it is specially designed to attack the problem of the physical nature of the dark energy. It will do it using several independent and complementary methods at the same time. One of them is the precise study of the spatial distribution of galaxies, and in particular, the BAO standard ruler. DES is a photometric survey, which means that its precision in the measurement of redshifts is limited, preventing the measurement of the Hubble parameter evolution. However, the evolution of the angular distance with redshift is possible, through the measurement of angular correlation functions (Seo & Eisenstein 2003; Padmanabhan et al. 2005; Blake & Bridle 2005; Padmanabhan et al. 2007; Crocce et al. 2011; Sánchez et al. 2011; Carnero et al. 2012; Seo et al. 2012; de Simoni et al. 2013).

Although DES will only measure BAO in the angular distribution of galaxies, a determination of the photometric redshift as precise as possible brings several benefits. It allows a finer tomography in the mapping of the BAO evolution with the redshift and makes the analysis cleaner, reducing the correlations between redshift bins. A sample of Luminous Red Galaxies (LRGs) would fit these requirements (Padmanabhan et al. 2005, 2007). LRGs are luminous and massive galaxies with a nearly uniform Spectral Energy Distribution (SED), but with a strong break at 4000 Å in the rest frame. These features allow a clean selection and an accurate determination of the redshift for this type of galaxies, even in photometric surveys. This selection has been done previously for imaging data at $z \lesssim 0.6$ (Padmanabhan et al. 2005). But the BAO scale has already been measured with high precision in this redshift range (e.g. Alam et al. (2017) and references therein). In order to go to higher redshifts, the selection criteria need to be redefined. The 4000 Å feature enters the i band at z = 0.75, and the methods used in previous selections are not valid anymore.

In this paper we describe the selection of a sample of red galaxies to measure BAO in DES, that includes, but is not limited to, LRGs. The selection is defined by two conditions. On the one hand, keep the determination of the photometric redshift as precise as possible. On the other hand, keep the galaxy density high enough to have a BAO measurement that is not limited by shot noise.

In order to guide our efforts to select an optimized sample for measuring BAO distance scales, we rely on Fisher matrix forecasts. See & Eisenstein (2007) provide a framework and simple formulae to predict the precision that one can achieve with a given set of galaxy data, given its number density, angular footprint, redshift uncertainty, and clustering amplitude. We fix the clustering amplitude, assuming a galaxy bias of b = 1.6 for all calculations. This is the bias found in Crocce et al. (2016) for a flux limited sample (i < 22.5) at redshifts $z \sim 0.9$, selected from DES Science Verification (SV) data. Since that redshift and magnitude are compatible with what we expect in this paper, we consider b = 1.6 a representative value. More precise measurements are expected for

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more biased samples, but the galaxy bias for any given sample is not known a priori and the redshift uncertainty and number density are the more dominant factors. Thus, we will test how Fisher matrix forecasts vary given the variations obtained for the number density and estimated redshift uncertainty given a set of color-magnitude cuts.

This paper, detailing the BAO sample selection, is one of a series describing the supporting work leading to the BAO measurement using DES Y1 data presented in DES Collaboration (2017) (hereafter DES-BAO-MAIN). As part of such series, one paper presents the mock galaxy catalogues, Avila et al. (2017) (hereafter DES-BAO-MOCKS). Gaztañaga et al. (2017) discusses in detail the photo-*z* validation, and we denote it DES-BAO-PHOTOZ. Chan et al. (2017), from now on DES-BAO- θ -METHOD, introduces the BAO extraction pipeline using a tomographic analysis of angular correlation functions, while Camacho et al. (2017) presents the study of the angular power spectrum (hereafter DES-BAO- ℓ -METHOD). Lastly, Ross et al. (2017a), in what follows referred to as DES-BAO- s_{\perp} -METHOD, introduced a novel technique to infer BAO distances using the three-dimensional correlation function binned in projected separations.

This paper is organized as follow: in section 2, a description of the main features of the DES-Y1 catalogue is given: in section 3, we give a detailed description of the selection cuts that define the data sample that has been used to measure the BAO scale in DES; section 4 contains a description of the procedure that has been developed and applied in DES in order to ensure the quality of the photometric redshift determination, and to determine its relation with the true redshift; section 5 describes the masking scheme and the treatment of the variable depth in the survey; section 6 is a description of the analysis and mitigation of observational systematic errors on the clustering measurement; and finally, section 7 describes the measured two-point correlation and cross-correlation functions and their evolution with redshift for the selected sample. We finish with our conclusions in section 8.

2 DES Y1 DATA

The BAO galaxy sample we will define in this work makes use of the first year of data (Y1) from the Dark Energy Survey. This photometric dataset has been produced using the Dark Energy Camera (DECam, Flaugher et al. (2015)) observations, processed and calibrated by the DES Data Management system (DESDM) (Sevilla et al. 2011; Mohr et al. 2012; Morganson et al. 2017) and finally curated, optimized and complemented into the Gold catalog (hereafter denoted 'Y1GOLD'), as described in Drlica-Wagner et al. (2017). For each band, single exposures are combined in *coadds* to achieve a higher depth. We keep track of the complex geometry that the combinations of these dithered exposures will create at each point in the sky in terms of observing conditions and survey properties. Objects are detected in chi-squared combinations of the *r*, *i* and *z* coadds to create the final coadd catalog (Szalay, Connolly & Szokoly 1999).

Y1GOLD covers a total footprint of more than 1800 deg²; this footprint is defined by a HEALPIX (Górski et al. 2005) map at resolution $N_{side} = 4096$ and includes only area with a minimum total exposure time of at least 90 seconds in each of the *griz* bands, and a valid calibration solution (see Drlica-Wagner et al. (2017) for details). This footprint is divided into several disjoint sub-regions which encompass the supernova survey areas, a region overlapping stripe 82 from the SDSS footprint (S82; Annis et al. (2014)) and a larger area overlapping with the South Pole Telescope coverage (SPT; Carlstrom et al. (2011)). Figure 1 shows the angular distribution of galaxies, selected as described in Section 3, that includes these two areas. A series of veto masks, including masks for bright stars and the Large Magellanic Cloud among others, reduce the area by $\sim 500 \text{ deg}^2$, leaving 1318 deg^2 suitable for LSS study. Other areas that are severely affected by imaging artifacts or otherwise have a high density of image artifacts are masked out as well. Section 5 provides a full account of the final mask used in combination with the final BAO sample. "Bad" regions information is propagated to the 'object' level by using the flags_badregion column in the catalog. Finally, individual objects which have been identified as being problematic by the DESDM processing or by the vetting process carried out by the scientists in the collaboration are flagged when configuring the catalog (this is done through the flags_gold column). All data we describe in this and in subsequent sections are drawn from quantities and maps released as part of the DES Y1 Gold catalog and are fully described in Drlica-Wagner et al. (2017).

The photometry used in this work comes mainly from two different sources:

• the SExtractor (Bertin & Arnouts (1996)) AUTO magnitudes, which are derived from the best matched elliptical aperture according to the coadd object elongation and angle in the sky, measured using the coadded object flux;

• Multi-Object Fitting (MOF) pipeline, which performs a multiepoch and multi-band fit of the shape and per-band fluxes directly on the single epoch exposures for each of the coadd objects, with additional neighboring light subtraction. This is described in more detail in Drlica-Wagner et al. (2017).

Using these photometric measurements, we will consider three different photometric redshift catalogues. Two of them are built using BPZ (Benítez 2000), a Bayesian template-fitting method, and another using a machine learning approach: the Directional Neighborhood Fitting (DNF) algorithm as described in De Vicente, Sánchez & Sevilla-Noarbe (2016). They are combined with the photometric quantities described above and used as follows:

• BPZ run with AUTO magnitudes (hereafter $z_{BPZ-AUTO}$) used for making the selection of the overall sample.

• BPZ run with MOF magnitudes (hereafter $z_{BPZ-MOF}$) used for redshift binning and transverse distance calculation, finally used as secondary catalogue to show the robustness of the analysis.

• DNF run with MOF magnitudes (hereafter $z_{DNF-MOF}$) used for redshift binning and transverse distance calculation, finally used as our fiducial catalogue.

We should note that BPZ with AUTO magnitudes is part of the DESDM data reduction pipeline and is available early on in the catalogue making. This explains why we used that particular combination for sample selection. We did not find, and do not expect, the relative optimization of the sample selection and cuts to depend much on the particular photo-z catalogue (but the final absolute error on BAO distance measurement does).

In Section 4, we summarize the validation performed to select and characterise the true redshift distributions of the binned samples, which is described in detail in DES-BAO-PHOTOZ.

Throughout our analysis we assume the redshift estimate of each galaxy to be the *mean* redshift of the redshift posterior for BPZ, or the predicted value for the object in the fitted hyper-plane from the DNF code (see De Vicente, Sánchez & Sevilla-Noarbe



Figure 1. Angular distribution and projected density of the DES-Y1 red galaxy sample described in this paper, and subsequently used for BAO measurements. The unmasked footprint comprises the two largest compact regions of the dataset: one in the southern hemisphere of 1203 deg², overlapping South Pole Telescope observations (SPT; Carlstrom et al. 2011), and 115 deg² near the celestial equator, overlapping with Stripe 82 (S82, Annis et al. 2014). The sample consists of about 1.3 million galaxies with photometric redshifts in the range [0.6 - 1.0] and constitutes the baseline for our DES Y1 BAO analysis.

Table 1. Complete description of the selection performed to obtain a sample dominated by red galaxies with a good compromise of photo-z accuracy and
number density, optimal for the BAO measurement presented in DES-BAO-MAIN. The redshifts of the resulting catalogue are then computed using different
codes (BPZ and DNF) as described in Sec 2. Therefore, any subsequent photo-z selection can be done either with z _{photo} from BPZ or DNF.

Keyword	Cut	Description
Gold	observations present in the Gold catalog	Drlica-Wagner et al. (2017)
Quality	flags_badregion < 4; flags_gold = 0	Sec.5; Sec.2
Footprint	1318 deg ² (1203 deg ² in SPT and 115 deg ² in S82)	Fig. 1 Sec.5
Color Outliers	$-1 < g_{\rm auto} - r_{\rm auto} < 3$	Sec. 3.1
	$-1 < r_{ m auto} - i_{ m auto} < 2.5$	Sec. 3.1
	$-1 < i_{ m auto} - z_{ m auto} < 2$	Sec. 3.1
Color Selection	$(i_{\text{auto}} - z_{\text{auto}}) + 2.0(r_{\text{auto}} - i_{\text{auto}}) > 1.7$	Sec. 3.3
Completeness	$i_{ m auto} < 22$	Sec. 3.1
Flux	$17.5 < i_{auto} < 19.0 + 3.0 z_{BPZ-AUTO}$	Sec. 3.3
Star-galaxy separation	$spread_model_i + (5/3) spreaderr_model_i > 0.007$	Sec. 3.2
Photo-z range	[0.6 - 1.0]	Sec. 4

(2016). Any potential biases from these estimates are calibrated as described in Section 4.

3 SAMPLE SELECTION

In this section, we describe the steps towards the construction of a red galaxy dominated sample, for BAO measurements, starting from the dataset described in Section 2. The selection is performed over the largest continuous regions of the survey at this point, namely SPT and S82. Objects are selected so that we avoid imaging artifacts and pernicious regions with foreground objects using the cuts on flags_badregion and flags_gold described therein. In the rest of this section we go into finer details on the flux, color and star-galaxy separation selection.

In Table 1, we summarise this sample selection, including references to the sections where these cuts are explained.

3.1 Flux and color outlier cuts

The flux-limit of the sample is set as

$$_{\rm auto} < 22. \tag{1}$$

Additionally, we remove the most luminous objects by making the cut $i_{auto} > 17.5$. The faint cut is selected as a compromise be-



Figure 2. Measurement of the trade off between area and number of objects as a function of magnitude limit and sample flux limit in Y1GOLD and SV. For a given i_{auto} -band "threshold" value we select all regions which have a deeper limiting magnitude that this value (10 σ depth limit > "threshold") and count the galaxies brighter than the "threshold" value over those regions. These should be complete samples at each threshold value. Number counts are shown normalized to their maximum in the figure.

tween the area lost and the homogeneous depth we would like to achieve. In Fig. 2 we show the normalized counts as a function of magnitude limit cut. For deeper magnitude limits, more objects are incorporated into the sample but the area reaching that depth is smaller. For comparison we include the same quantity in Science Verification Data, which is deeper than Y1 but much smaller area, that justifies the sample flux limit of $i_{auto} < 22.5$ in Crocce et al. (2016). The curve shows a plateau in the range $22 \leq i_{auto} \leq 22.4$, with variations of about 5%. However the photo-*z* performance (not shown), particularly at high redshift, degrades rapidly for fainter objects. Therefore we decided to stay at the bright end of this range ($i_{auto} = 22$).

Color outliers which are either unphysical or from special samples (Solar System objects, high redshift quasars) are removed as well, to avoid extraneous photo-z populations in the sample (see Table 1).

3.2 Star-Galaxy Separation

Removing stars from the galaxy sample is an essential step to avoid the dampening of the BAO signal-to-noise Carnero et al. (2012) or the introduction of spurious power on large scales (Ross et al. 2011a). Stellar contamination affects the broad shape of the measurement and so we want to minimise it to be able to fit the BAO template properly. However, it does not appreciably affect the location of the BAO feature, so we don't need to push for 100% purity. Any residual contamination is then taken care of by using the weighting scheme detailed in Section 6.

In this work we have used the default star-galaxy classification scheme described in Drlica-Wagner et al. (2017), based on the *i*-band coadd magnitude spread_model_i and its associated error spreaderr_model_i, from SExtractor. This classifier was developed using as truth tables data from COSMOS (Leauthaud et al. 2007), GOOD-S (Giavalisco et al. 2004) and VVDS (Le Fèvre et al. 2005) overlapping Y1GOLD, and subsequently tested against CFHTLenS (Erben et al. 2013). The combination spread_model_i + (5.0/3.0)spreaderr_model_i > 0.005 is suggested for high-confidence galaxies as a baseline for Y1GOLD. A detailed follow up analysis of star-galaxy separation is given in



Figure 3. Contamination of galaxy sample from stars as a function of redshift and star-galaxy separation threshold, as measured using galaxy density vs stellar density plots (from a pure stellar sample). The MODEST classifier is defined in Drlica-Wagner et al. (2017) as the default star galaxy classifier (based on spread_model and wavg_spread_model). 'BAO classifier' stands for a cut in spread_model_i + (5.0/3.0)spreaderr_model_i. A threshold of 0.007 provides an important decrease of contamination with a minor adjustment in the number of galaxies, which becomes significantly more severe at higher thresholds for a very similar purity. The redshift binning here uses $z_{\rm BPZ-AUTO}$.

Sevilla-Noarbe et al. (2017). Here instead we decided to modify slightly this proposed cut in order to increase the purity of the sample (from 95% to 97 - 98%), at the cost of losing approximately 3% of the objects, by making the following selection:

 $pread_model_i + (5.0/3.0) preaderr_model_i > 0.007.$

In Fig. 3 we show the estimated star sample contamination for different thresholds of this cut, using the relation between galaxy density and a map of stellar density built from Y1GOLD (a methodology that is described in detail in section 6). A threshold of 0.007reduces the contamination level to less than 5% across the redshift range of interest. In Table 2 we report a consistent or smaller level of stellar contamination, using a similar estimation, in the catalogues with MOF photometry, both for BPZ and DNF (see Sec. 6). In Fig. 5 we also include in the middle figure the track from the stellar locus, which showcases the reason why the first two redshift bins are more affected by stellar contamination, as it crosses the elliptical templates at these redshifts. To further illustrate this, in Fig. 4 we show the distribution of the mean photometric redshifts for stars (selected using the criterion |wavg_spread_model_i| < 0.002, a more accurate variant of spread_model_i using singleepoch, suitable for moderate to bright magnitude ranges) showcasing how they will contaminate preferentially the second redshift bin, following the same trend as shown in Table 2.

3.3 Selecting Red Luminous Galaxies for BAO

Next we want to select from Y1GOLD a sample dominated by luminous red galaxies, given that the typical photo-*z* estimates for these are more accurate than for the average galaxy population, thanks to the 4000 Å Balmer break in their spectra. This feature makes redshift determination easier even with broad-band photometry (Padmanabhan et al. 2005). In addition we want our BAO sample to cover redshifts larger than 0.6 as there are already very precise BAO measurements for z < 0.6, see e.g. Cuesta et al. (2016); Ross et al. (2017b); Beutler et al. (2017).



Figure 4. Photometric redshift distribution of stars selected morphologically and passing the same cuts described in Table 1. The redshift value z_{phot} is the mean from the pdf of $z_{BPZ-AUTO}$, which was used for the overall sample selection in Section 3.

We have tested that, while a very stringent selection can be done to yield minimal photo-z errors, e.g. with the redMaGiC algorithm (Rozo et al. 2016), it does not lead to optimal BAO constraints because the sample ends up being very sparse, with $\sim 200,000$ galaxies in Y1GOLD at z > 0.6 (Elvin-Poole et al. 2017).

Instead we will follow an alternative path and apply a standard selection in color-color space to isolate red galaxies at high redshift, balancing photo-z accuracy and number density with a BAO figure-of-merit in mind.

In Figure 5 we show the evolution in redshift of the eight spectral templates used in BPZ, which includes one typical red elliptical galaxy, two spirals and five blue irregulars/starbursts (color coded) based on Coleman, Wu & Weedman (1980) and Kinney et al. (1996). We compute the expected observed DES broad-band magnitudes for these templates as a function of redshift and show them in different color-color combinations. The tracks are evolved from z = 0 to z = 2.0 in steps of 0.1 (marked with dots). We will use these to define cuts in color-color space which allow isolating the red templates, which typically occupy a distinct region in color-color space.

A model of a red elliptical galaxy is shown in Figure 6, where it appears redshifted to z = 0.4, 0.8, 1.15, where the notable 4000 Å break crosses from $g \rightarrow r$, $r \rightarrow i$ and $i \rightarrow z$. This suggests that for z > 0.6 the strongest evolution in color will be for i - z and r - i, and hence we will focus in this combination. Note how the transition of the 4000 Å break from one band to another abruptly bends the color-color tracks in Figure 5. However, this applies mainly to elliptical templates, and recent star formation will dampen this effect.

Thus, in order to maximize the signal-to-noise of the BAO measurement, a color cut is applied to the sample in the form,

$$(i_{\text{auto}} - z_{\text{auto}}) + a_1(r_{\text{auto}} - i_{\text{auto}}) > a_2.$$

$$(2)$$

The cut was chosen in this form as it allows us to select only the reddest galaxies (see Figure 5) which are the ones with lower uncertainties in their photometric redshift determination and still present a high enough number density.

Samples were produced across a grid of a_1 and a_2 values, calculating the number of galaxies $N_{\rm gal}$ and a mean width of the photo-z distribution $\sigma_z/(1+z)$ for each sample, after splitting the galaxy in tomographic bins. For BPZ we estimated σ_z averaging in

Table 2. Characteristics of the DES Y1 BAO sample, as a function of redshift. Results are shown for a selection of the sample in bins according to DNF photo-z ($z_{\rm phot}$) estimate in top of the table and BPZ in the bottom, both with MOF photometry. Here $\bar{z} = \langle z_{true} \rangle$ is the mean true redshift, σ_{68} and W_{68} are the 68% confidence widths of ($z_{\rm phot} - z_{true}$)/(1 + z_{true}) and z_{true} respectively, all estimated from COSMOS-DES validation with SVC correction, as detailed in Sec. 4 and Fig. 7. $f_{\rm star}$ is the estimated stellar contamination fraction, see Sec. 6

DNF	$N_{\rm gal}$	bias	\overline{z}	σ_{68}	W_{68}	$f_{\rm star}$
$\begin{array}{c} 0.6-0.7\\ 0.7-0.8\\ 0.8-0.9\\ 0.9-1.0\end{array}$	386057 353789 330959 229395	$\begin{array}{c} 1.81 \pm 0.05 \\ 1.77 \pm 0.05 \\ 1.78 \pm 0.05 \\ 2.05 \pm 0.06 \end{array}$	0.652 0.739 0.844 0.936	0.023 0.028 0.029 0.036	0.047 0.068 0.060 0.067	0.004 0.037 0.012 0.015
BPZ	$N_{\rm gal}$	bias	\overline{z}	σ_{68}	W_{68}	$f_{\rm star}$

each tomographic bin the width of the individual redshifts posterior distributions (PDFs) provided per galaxy.

The BAO forecast using the algorithm of Seo & Eisenstein (2007) is then run for the N_{gal} and $\sigma_z/(1+z)$ of each sample and final values of a_1 and a_2 are selected to minimise the forecasted BAO uncertainty, finding a balance between galaxy number density and redshift uncertainty. In order to give a sense for the sensitivity of such process, we note there is a slight degeneracy when increasing a_1 and a_2 simultaneously, resulting in similar forecasted BAO uncertainties. However deviations from this degeneracy direction lead to significant degradation in the forecasted error. For example, doubling a_1 leads to a degradation of the forecasted error by approximately 0.01 (from 5% to 6% roughly). The values used in this analysis are $a_1 = 2.0$, $a_2 = 1.7$. Figure 5 shows the color cut in the central panel, where the shadowed region is excluded from the sample.

To further minimize the forecasted BAO uncertainty, an additional, redshift dependent magnitude cut is applied to the sample as a second step. This applies a cut to i_{auto} at low redshift which is stricter than the global $i_{auto} < 22$ cut (at lower redshift the sample is sufficiently abundant that one can still select brighter galaxies, with better photo-z, and still be sample variance dominated). The cut is in the form,

$$i_{\text{auto}} < a_3 + a_4 z. \tag{3}$$

As with the color cut in Eq. 2, this is designed to find a sample that balances redshift uncertainty with number density, to minimise the forecasted BAO error. The BAO forecast error was minimised at the values $a_3 = 19$ and $a_4 = 3$ and this cut was applied to the sample. We find that the forecasted error improves by $\sim 15\%$ when introducing the redshift dependent flux limit as opposed to a global $i_{\text{auto}} < 22$ cut.

The final forecasted uncertainty on angular diameter distance combining all the tomographic bins is $\sim 4.7\%$. Note that the discussion in this section only has as a goal the definition of the sample. The real data analysis with the sample defined here, and the final BAO error achieved, will of course depend in many other variables that were not considered up to this point. Such as the quality of photometric redshift errors, analysis and mitigation of systemat-



Figure 5. Evolution of BPZ templates in color-color space. Each dot corresponds to a different redshift in steps of 0.1, ranging from z = 0.0 to z = 2.0. The shadowed region in the central panel is excluded from the sample. The black dots indicate the position of z = 0.6 (triangles), and z = 1.0 (squares) for the two reddest templates. Also shown, for reference, is the stellar locus as a purple dashed line.



Figure 6. Elliptical model spectrum used in template-based fitting code BPZ. Overplotted are the DES response filters g,r,i,z. The template has been redshifted to z = 0.4, 0.8, 1.15, where the notable 4000 Å break crosses from $q \rightarrow r, r \rightarrow i$ and $i \rightarrow z$.

ics, use of the full covariance and optimized BAO extraction methods.

We note however that the forecasted error obtained in this section is in fact quite close to the final BAO error obtained in DES-BAO-MAIN. In the following sections we discuss the various components that will enter the real data analysis, starting with the validation of photometric redsfhit errors and the estimate of redshift distributions.

4 PHOTOMETRIC REDSHIFTS

The photometric redshifts used for redshift binning and transverse distance computations in our fiducial analyses are derived using the Directional Neighborhood Fitting (DNF) algorithm (De Vicente, Sánchez & Sevilla-Noarbe 2016), which is trained with public spectroscopic samples as detailed in Hoyle et al. (2017). For comparison we also discuss below the Bayesian Photometric Redshift (BPZ) (Benítez 2000) which we find slightly less performant in terms of the error with respect to "true" redshift values (see below). In both cases we use MOF photometry which provides $\sim 10-20\%$ more accurate photo-*z* estimates with respect to the equivalent estimates using SExtractor MAG_AUTO quantities from coadd photometry. In this section we summarise the steps taken to arrive at these choices, based on a validation against data over the COSMOS field.

We recall that throughout this work we use the individual object's mean photo-z from BPZ (not to be confused with the mean value $\bar{z} = \langle z \rangle$ of the sample) and the predicted value in the fitted hyper-plane from the DNF code, as our point estimate for galaxy redshifts. As for the estimates of the N(z) from the photo-z codes, for comparison with our fiducial choice based on the COS-MOS narrow band p(z), we will use the stacking of Monte Carlo realisations of the posterior redshift distributions p(z) for the BPZ estimates, or the stacking from the nearest neighbour redshifts from the training sample, in the case of DNF (henceforth we'll call these stack N(z)). Figure 7 shows the stack N(z) (yellow histograms) in all 4 redshift bins for our fiducial DNF photo-z analysis.

4.1 COSMOS Validation

As detailed in DES-BAO-PHOTOZ, we check the performance of each code by using redshifts in the COSMOS field (which are not part of the training set in the case of DNF), following the procedure outlined in Hoyle et al. (2017). These redshifts are either spectroscopic or accurate ($\sigma_{68} < 0.01$) 30-band photo-*z* estimates from Laigle et al. (2016). Both validation samples give consistent results in our case because the samples under study are relatively bright.

The COSMOS field is not part of the DES survey. However a few select exposures were done by DECam which were processed by DESDM using the main survey pipeline. We call this sample DES-COSMOS. Because the COSMOS area is small (2 square degrees) and DECam COSMOS images were deeper and not taken as part of the main DES-Y1 Survey, we need to first resample the DES-COSMOS photometry to make it representative of the full DES Y1 samples that we select in our BAO analysis. Hence we add noise to the fluxes in the DES-COSMOS catalog to match the



Figure 7. Normalised redshift distributions for our different tomographic bins of DNF-MOF photo-z. Stack N(z) are shown for the full DES-Y1 BAO sample (yellow histograms). The black histogram (with Poisson error bars) shows the raw 30-band photo-z from the COSMOS-DES validation sample. Magenta lines shows the same sample corrected by sample variance cancellation (SVC, see text), which is our fiducial estimate. The labels show the values of W_{68} , σ_{68} and $\Delta z = \langle z_{stack} \rangle - \langle z \rangle$ and in each case, see also Table 2.

noise properties of the fluxes in the DES-Y1 BAO sample, this is what we refer to as resampled photometry. Then for each galaxy in the DES-Y1 BAO sample, we select the galaxy in DES-COSMOS whose resampled flux returns a minimum χ^2 when compared to the DES-Y1 BAO flux (the χ^2 combines all bands, g, r, i and z). This is done for every galaxy in the DES-Y1 BAO sample to make up the 'COSMOS-Validation' catalog, which by construction has colors matching those in the DES-Y1 BAO sample. The "true" redshift is retrieved from the spectroscopic/30-band photo-z of this match.

We then run the DNF photo-z code over the COSMOS-Validation catalog to select 4 redshift bin samples in the same way as we did for the full DES-Y1 BAO sample. We use the "true" redshifts from the COSMOS-Validation catalogs to estimate the N(z)in each redshift bin by normalising the histogram of these true redshifts.

Results are shown as histograms in Figure 7, which are compared to the stack N(z) from the photo-z code, for reference. The black histograms show large fluctuations which are caused by real individual large scale structures in the COSMOS field. This can be seen by visual inspection of the maps. This sampling variance comes from the relatively small size of the COSMOS validation region. There is also a shot-noise component, indicated by the error bars over the black dots, but it is smaller. In the next section, we briefly describe the methodology to correct for this to be able to make use of this validation sample effectively.

4.2 Sample variance correction

As detailed in DES-BAO-PHOTOZ we apply a sampling variance correction (SVC) to the data and test this method with the Halogen mocks described in DES-BAO-MOCKS. In what follows we provide a summary of such process and its main results.

We use the VIPERS catalog (Scodeggio et al. 2016), which spans 24 square degrees to i < 22.5, to estimate the sampling variance effects in the above COSMOS validation. After correcting VIPERS for target, color and spectroscopic incompleteness we select galaxies in a similar way as done in section 3. We then use the VIPERS redshifts to estimate the true N(z) distribution of the parent DES-COSMOS sample (before we select in photometric redshifts). The ratio of the N(z) in the DES-COSMOS sample to the one in VIPERS gives a sample variance correction that needs to be applied to the N(z) in each of the tomographic bins. Figure 7 shows the SVC-corrected version of the raw COS-MOS catalog in magenta. As shown in this figure the resulting distribution is much smoother than the original raw measurements (black histograms). This by itself indicates that SVC is working well. Tests in simulations show that this SVC method is unbiased and reduces the errors in the mean and variance of the N(z) distribution by up to a factor of two. Similar results are found for different binnings in redshift.

4.3 Photo-*z* validation results

In Table 2 we show the values of σ_{68} , which corresponds to the 68% interval of values in the distribution of $(z_{photo} - z_{true})/(1 + z_{true})$ around its median value, where z_{photo} is the photo-z from DNF (z_{mean} above) and z_{true} is the redshift from the COSMOS validation sample corrected by SVC. We also show W_{68} and \bar{z} which are the 68% interval and mean redshift in the z_{true} distribution for each redshift bin. The corresponding values for the stack N(z) and raw N(z) are also shown in the labels of Figure 7. Δz in the label inset shows the difference $\Delta z = \langle z_{stack} \rangle - \langle z \rangle$, where $\langle z_{stack} \rangle$ is the mean stack redshifts for DES-Y1, shown in the top label.

In DES-BAO-PHOTOZ we present a comparison of the quantities shown in Table 2 with and without SVC and also between COSMOS validation and N(z) from DNF stacks (see also labels of Figure 7). The validation errors and biases in these values are also presented but we anticipate that they are subdominant for the BAO analysis, which instead is dominated by the limited size of the DES Y1 footprint. In DES-BAO-PHOTOZ we present results for the COSMOS subsample with only spectroscopic redshifts, which shows a good agreement for these quantities when using COSMOS 30-band photo-z instead of the spectroscopic redshifts. We also include a comparison with BPZ photo-z (see also Table 2) and results for different photo-z with coadd photometry. The values of W_{68} and σ_{68} are always smaller (by 10-20%) for DNF with MOF photometry, which is therefore used as our fiducial photo-z sample.

The fiducial N(z) used in the main BAO analysis are the ones from COSMOS with SVC (magenta lines in Figure 7).

5 ANGULAR MASK

We build our mask as a combination of thresholds/constraints on basic survey observation properties, conditions due to our particular sample selection, and restrictions to avoid potential clustering systematics. In summary,

• We start by combining the Y1GOLD Footprint and Bad regions mask, both of which are described in Drlica-Wagner et al. (2017). The Footprint mask imposes minimum total exposure times, valid stellar locus regression¹ (SLR) calibration solutions and basic coverage fractions. The Bad Regions mask removes at different levels various catalog artifacts, regions around bright stars and large foreground objects. In particular, for the later we remove everything with flag bit > 2 in Table 5 of Drlica-Wagner et al. (2017), corresponding to regions around bright starts in the 2MASS catalogue (Skrutskie et al. 2006). • We introduce coordinate cuts to select only the wide area parts of the surveys, namely those overlapping SPT (roughly with $300 < RA(\deg) < 99.6$ and $-40 < DEC(\deg) < -60$) and S82 (with $317.5 < RA(\deg) < 360$ and $-1.76 < DEC(\deg) < 1.79$). This removes small and disjoint regions which are part of the Supernova survey and two auxiliary fields used for photo-*z* calibration and star-galaxy separation tests (COSMOS and VVDS-14h), which do not contribute to our clustering signal at BAO scales.

• Pixelized maps of the survey coverage fraction were created at a HEALPIX resolution of $N_{\rm side} = 4096$ (area = 0.73 arcmin²) by calculating the fraction of high resolution subpixels ($N_{\rm side} = 32768$, area = 0.01 arcmin²) that were contained within the original mangle mask (see Drlica-Wagner et al. (2017) for a description of the later). Since our color selection requires observations in all four *griz* bands we use the coverage maps to enforce that all pixels considered (at resolution 4096) show at least 80% coverage in each band. Furthermore we then use the minimum coverage across all four bands to down-weight the given pixel when generating random distributions, see Sec. 7.

• In order to match the global magnitude cut of the sample and ensure it is complete across our analysis footprint, we select regions with 10σ limiting depth of $i_{auto} > 22$, where the depths are calculated according to the procedure presented in Drlica-Wagner et al. (2017).

• Since we want to reliably impose the color cut defined in Eq. (2) and Table 2, we consider only areas with limiting depth in the corresponding bands large enough to measure it. Given that we are already imposing $i_{\rm auto}$ depth greater than 22, the new condition implies keeping only the regions with 10σ limiting magnitudes $(2r_{\rm auto} - z_{\rm auto}) < 23.7$, or equivalently those with $z_{\rm auto} > 2r_{\rm auto} - 23.7$.

• As a result of our analysis of observational systematics in Sec. 6, we identify that galaxy number density in regions of high *z*-band seeing shows an anomalous behaviour. To isolate this out we remove areas with *z*-band seeing greater than 1 arc-second (that amounts to 71 deg², or 5% of the footprint)

 \bullet Lastly we also remove a patch of $18\,{\rm deg}^2$ over which the airmass computation was corrupted.

The resulting footprint occupies 1318 deg^2 and is shown in Fig. 1.

6 MITIGATION OF OBSERVATIONAL SYSTEMATIC EFFECTS

We have tested for observational systematics in a manner similar to Elvin-Poole et al. (2017), which builds upon work in DES Science Verification Data (Crocce et al. 2016) and other surveys (e.g. Ross et al. (2011a); Ho et al. (2012)).

Generically, we test the dependence of the galaxy density against survey properties (SPs). We expect there to be no dependence if SPs do not introduce density fluctuations in our sample beyond those already accounted for by the masking process. We have used the same set of SP maps as in Elvin-Poole et al. (2017), namely :

¹ This is a complementary calibration technique used for the construction of Y1GOLD making use of the distinct color locus occupied by stars to perform relative additional calibration between bands.

- 10σ limiting depth in band
- full width half maximum of point sources ("seeing")
- total exposure time
- total sky brightness,
- atmospheric airmass,

all of them in each of the four bands griz, in addition to Galactic extinction and stellar contamination (refer to Elvin-Poole et al. (2017) for a detailed explanation on how the stellar density map is constructed from Y1GOLD data). We find that the relevant systematics are stellar density, PSF FWHM, and the image depth. We outline the tests that reveal this and how we apply weights to counter their effect in what follows.

We found the most important systematic effect, in terms of its impact on the measured clustering, to be the stellar density. In the top panel of Fig. 8 we find positive trends when comparing the number density of our 'galaxy' sample as a function of the stellar number density (n_{star}) . Our interpretation is that there are stars in our sample. Assuming these contaminating stars follow the same spatial distribution as the stars we use to create our stellar density map, this stellar contamination will produce a linear relationship between the density of our galaxy sample and the stellar density. In this scenario, the value of the best-fit trend where the number density of stars, $n_{\rm star},$ is 0 is then the purity of the sample. We find the results are indeed consistent with a linear relationship, as illustrated in the top panel of Fig. 8. The stellar contamination, f_{star} , that can be determined from these plots is listed in Table 2. The stellar contamination varies significantly with redshift, as expected given the proximity of the stellar locus to the red sequence as a function of redshift. Thus, we measure the stellar contamination in $\Delta_z = 0.05$ bin widths and use a cubic spline interpolation in order to obtain the stellar contamination at any given redshift. This allows us to assign a weight to each galaxy given by,

$$w(f_{\text{star}}(z)) = ((1 - f_{\text{star}}(z)) + n_{\text{star}}f_{\text{star}}(z)/\langle n_{\text{star}}\rangle)^{-1},$$
 (4)

where $n_{\rm star}$ is the stellar density that depends on angular location and $\langle n_{\rm star} \rangle$ is the mean stellar density over the DES-Y1 footprint.

Note that we repeat the fitting procedure for each photo-z catalogue, hence redshift here means either $z_{\rm DNF-MOF}$ or $z_{\rm BPZ-MOF}$. From Fig. 8 it seems that the measurements are a bit noisy. However this procedure helps us resolve the peak in the stellar contamination of five per cent at $z \sim 0.78$. The uncertainty on each fit is ~ 0.01 , which is consistent with the scatter we find in the values of $f_{\rm star}$ per bin. The spline simply interpolates between the best-fit values.

We also add weights based on fits against relationships with the mean *i*-band PSF FWHM (seeing, which we denote as s_i) and the *g*-band depth (d_g .) The dependencies we find are purely empirical as we lack any more fundamental understanding for how these correlations develop. They must result from the complicated intersection of our color/magnitude selection and the photometric redshift algorithm. For the seeing, we do not find a strong dependence on redshift and thus use the full sample to define the seeing dependent weight

$$w(s_i) = (A_s + B_s s_i)^{-1}, (5)$$

where A_s and B_s are simply the intercept and slope of the bestfit linear relationship, shown in the middle panel of Fig. 8. The coefficients we use are $A_i = 0.782$ and $B_i = 0.0625$. For the g-band depth, we fit linear relationships in redshift bins $\Delta_z = 0.1$ and again use a cubic spline interpolation in order to obtain a weight at any redshift

$$w(d_g, z) = (C(z) + d_g(1 - C(z))/\langle d_g \rangle)^{-1}, \qquad (6)$$

where C(z) is the interpolated result for the value of the linearfit where $d_g = 0$. The relationships as a function of redshift and the linear best-fit models are shown in the bottom panel of Fig. 8. The total systematic weight, w_{sys} , is thus multiplication of the three weights

$$w_{\rm sys} = w(f_{\rm star}(z))w(s_i)w(d_g, z) \tag{7}$$

In the following section, we test the impact of these weights on the measured clustering, and determine their total potential impact. In DES-BAO-MAIN, we show that the weights have minimal impact on the BAO scale measurements and that our treatment is thus sufficient for such measurements. Our treatment is not as comprehensive as Elvin-Poole et al. (2017), and thus further study might be required when using the sample defined here for non-BAO applications.

7 TWO-POINT CLUSTERING

In this section we describe the basic two-point clustering properties of the samples previously defined. We concentrate on large-scales where the BAO signal resides, and the sample using $z_{\rm DNF-MOF}$ photometric redshifts which is the default one used in DES-BAO-MAIN.

We compute the angular correlation function $w(\theta)$ of the sample, split into four redshift bins, using the standard Landy-Szalay estimator (Landy & Szalay 1993),

$$w(\theta) = \frac{DD(\theta) - 2DR(\theta) + RR(\theta)}{RR(\theta)}$$
(8)

as implemented in the CUTE software² (Alonso 2012), where $DD(\theta)$, $DR(\theta)$ and $RR(\theta)$ refer to normalized pair-counts of Data (D) and Random (R) points, separated by an angular aperture θ . Random points are uniformly distributed across the footprint defined by our mask (albeit downsampled following the fractional coverage of each pixel, described in Sec. 5), with an abundance twenty times larger than that of the data in each given bin. For the fits and χ^2 values quoted in this section we always consider 16 angular-bins linearly spaced between $\theta = 0.45 \text{ deg}$ and $\theta = 4.95 \text{ deg}$, matching the scale cuts in the BAO analysis using $w(\theta)$ of DES-BAO-MAIN. We compute pair-counts in angular aperture bins of width 0.3 deg in order to reduce the covariance between the measurements. The covariance matrix is derived from 1800 Halogen mocks, described in detail in DES-BAO-MOCKS.

The expected noise in the inverse covariance from the finite number of realisations (Hartlap, Simon & Schneider 2007) and the translation of that into the variance of derived parameters (Dodelson & Schneider 2013) is negligible given the size of our data vector (16 angular measurements per tomographic redshift bin) and the number of model parameters (one bias per bin). For instance the increased error in derived best-fit biases in any given bin would be sub-percent. The change in the full $\sqrt{\chi^2}$ is ~ 3.7% (16x4 datapoints, see the discussion below). We therefore neglect these corrections in this section.

Figure 9 shows the impact of the systematic weights on the measured angular clustering in terms of the difference Δw between the pre-weighted correlation function w and the post-weighted one w_{weighted} , relative to the statistical error σ_w (i.e. neglecting all covariance). To compare this against the expected amplitude of the

² https://github.com/damonge/CUTE

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Figure 9. The impact of the systematic weights on each redshift bin, shown by the differential angular correlations, with and without weights applied, relative to the uncertainty. One can see that the weights make the biggest difference for the 0.7 < z < 0.8 bin, which is the redshift range with the greatest stellar contamination. The thick solid line displays the BAO feature in similar units, $(w_{BAO} - w_{no BAO})/\sigma_w$, for the second tomographic bin as an example (different bins show similar BAO strength but displaced slightly in the angular coordinate). The systematic weights only modify the underlying smooth shape, and do not have a sharp feature at BAO scales.

BAO feature at this scales we also display in thick solid black line the theoretical angular correlation function with and without BAO, for the second tomographic bin for concreteness, relative to the statistical errors. The corrections are all at the same level (or smaller) than the expected BAO signal.

The weights have the largest impact in terms of clustering amplitude for the redshift bin 0.7 < z < 0.8, which is the redshift range with the largest stellar contamination (~ 4%, see Table 2), although never exceeding one σ_w . For the remaining bins the change in the correlation functions are within 1/4 of σ_w . We can assess quantitatively the total potential impact of the weights by calculating $\chi^2_{\rm sys} = \Delta w(\theta)^t C^{-1} \Delta w(\theta)$; the square-root of this number is an upper bound in the impact, in terms of number of σ 's, that the weights could have on the determination of any model parameter.

In the range 0.45 deg $< \theta < 4.95$ deg, with 16 data-points, we find $\chi^2_{\rm sys} = 0.1, 1.35, 0.2$ and 0.5 respectively for each tomographic bin separately (showing that for example best-fit bias derived solely from the 2nd tomographic bin can be shifted by more than one sigma if weights are uncorrected for). More interestingly, for the four bins combined and including the full covariance matrix, we find $\chi^2_{\rm sys} = 1.35$. This implies a maximum impact of 1.16σ in a derived global parameter such as the angular diameter distance measurement. This maximum threshold is well above the actual impact of the weights in D_A/r_s found in DES-BAO-MAIN, which is $0.125\sigma_{D_A/r_s}$ (see Table 5 in that reference). We consider this an indication that the particular shape of the BAO feature is not easily reproducible by contaminants, and is therefore largely insensitive to such corrections, which is consistent with previous analyses (Ross et al. 2017b).

Figure 10 displays the auto-correlation function (including observational systematic weights) of 4 tomographic bins of width $\Delta z_{photo} = 0.1$ between $0.6 \leq z_{photo} \leq 1.0$. Data at z > 0.8appear to show significant BAO features. Best fit biases, derived 1σ errors and their corresponding χ^2 values are reported as inset

Figure 8. The galaxy density vs. potential systematic relationship used to define weights that we apply to clustering measurements. *Top panel:* The galaxy density versus stellar density in four photometric redshift bins. The linear fits are used to determine the stellar contamination. The χ^2 values for the fits are 9.7, 10.0, 3.5, and 14.3 (8 degrees of freedom). *Middle panel:* The galaxy density versus the mean *i*-band seeing for our full sample. The inverse linear fit is used to define weights applied to clustering measurements. The χ^2 is 7.7 (8 degrees of freedom) and the coefficients are 0.788 and 0.0618. *Bottom panel:* The galaxy density versus for each freedom and the coefficients are 0.788 and 0.0618. *Bottom panel:* The galaxy density versus *g*-band depth in four photometric redshift bins. The coefficients are interpolated as a function of redshift and used to define weights to be used in the clustering measurements. The χ^2 values for the fits, given 8 degrees of freedom, are 7.7, 8.9, 12.7, and 6.1. The slopes are (-0.0256, 0.0320, 0.103, 0.0609).



Figure 10. Angular correlation function in four redshift bins, for galaxies selected with $z_{\text{DNF}-\text{MOF}}$. Symbols with error bars show the clustering of galaxy sample corrected for the most relevant systematics. Dashed line displays a model using linear theory with an extra damping of the BAO feature due to nonlinearities, and a linear bias fitted to the data (whose best fit value is reported in the inset labels). We consider 16 data-points and one fitting parameter in each case (dof=15). Note that the points are very covariant, which might explain the visual mismatch in the first tomographic bin that nonetheless retains a good χ^2/dof .



Figure 11. Angular cross-correlation functions of the four tomographic bins in $0.6 < z_{\text{photo}} < 1.0$, see Fig. 10, for galaxies selected according to $z_{\text{DNF-MOF}}$. The model prediction shown with dashed lines assumes a bias equal to the geometric mean of the auto-correlation fits, i.e. $b_{ij} = \sqrt{b_i b_j}$, and is basically proportional to the overlap of redshift distributions, which are shown in the bottom right panel.

panels and in Table 2. The model displayed assumes linear theory and the MICE cosmology³ (Fosalba et al. 2015; Crocce et al. 2015), with an extra damping of the BAO feature, see DES-BAO- θ -METHOD for details. The χ^2 /dof are all of order ~ 1 or better, showing that these are indeed good fits given the covariance of the data. In Table 2 we also report best fit bias values for a split of the sample into four tomographic bins using the BPZ_{MOF} photo-*z*, showing no discrepancies.

As a further test of the clustering signal, as well as the tails of the photo-z distributions, we show in Fig. 11 the cross-correlation between different bins. The overploted models were derived using the redshift distributions of the corresponding bins and assume a bias equal to the geometric mean of the tomographic bins,

$$w_{ij}(\theta) = b_{ij}^2 \int \int dz \, d\tilde{z} n_i(z) n_j(\tilde{z}) D(z) D(\tilde{z}) \xi(r_\theta) \quad (9)$$

where $r_{\theta}^2 = r(z)^2 + r(\tilde{z})^2 - 2r(z)r(\tilde{z})\cos\theta$ and $b_{ij}^2 = b_i b_j$. In Eq. (9) we denote ξ the spatial correlation function computed in linear theory at z = 0. The error bar displayed and the reported χ^2 values are obtained with a theoretical covariance matrix designed to match the Halogen mocks covariance of the autocorrelations (i.e. matching the bias and shot noise and area of the mocks). Detailed formulae and tests of this theory covariance are given in a companion paper, DES-BAO- θ -METHOD (see also Crocce, Cabré & Gaztañaga (2011); Ross et al. (2011b); Salazar-Albornoz et al. (2014)). However when we test the χ^2 values of the auto-correlations against the best-fit model⁴ using this theory covariance instead of the one derived from the mocks we find considerably larger χ^2 values: $r_i \equiv \chi^2_{i,\text{theory-cov}}/\chi^2_{i,\text{mocks-cov}} =$ 1.46, 1.37, 1.37, 1.47 for auto-correlations in bin i = 1 to 4, respectively. We propagate this uncertainty to the cross-correlations by dividing $\chi^2_{ij,\text{theory-cov}}$ by $\sqrt{r_i r_j}$.

Overall the cross-correlations show a good match to the model, which is sensitive to the tails of the redshift distributions and the geometric mean bias. The χ^2 /dof are ~ 1. The non-adjacent bin 1 × 3 (where the expected clustering signal is negligible) shows an excess correlation on very large-scales. This most probably indicate a residual systematic and not a problem of the photo-z distributions.

The large χ^2 values in some of the cross-correlations (bins 2×3 and 3×4) are driven by the non-diagonal structure of the covariance matrix rather than a mismatch between the best-fit bias of the cross-correlation b_{ij} compared to the geometrical mean of the auto-correlation biases. For example, for 2×3 the best-fit bias from $w_{2\times3}$ is only 2% larger than $\sqrt{b_2b_3}$ (and the corresponding χ^2 change sub-percent). On the other hand, the χ^2 of the cross-correlation drops to 0.4 if we only consider a diagonal covariance matrix. Similarly $\chi^2_{3\times4}$ drops to 1.28 from 2 using a diagonal covariance matrix. Overall, we conclude there is a fairly good match between the implications of the overlap of redshift distributions and the cross-correlation clustering signal.

In Figure 12 we show $\xi(s_{perp})$ which is the three-dimensional correlation function binned only in projected physical separations.



Figure 12. Three-dimensional correlation function binned in projected pair separations. We use projected separations because radial pairs are damped due to photo-*z* mixing. The dashed line is the best fit model assuming linear bias and a smeared BAO feature, as discussed in detail in DES-BAO-MAIN.

To compute this correlation we converted (photometric) redshift and angles to physical distances assuming MICE cosmology. This yields a three-dimensional map of the galaxies in comoving coordinates. Random points are distributed in this volume with the same angular distribution as the angular mask defined in section 5, and used for $w(\theta)$, and drawing redshifts randomly from the galaxies themselves. Pair counts are then computed and binned in projected separations. A full detail of such procedure is given in DES-BAO-MAIN as well as in Ross et al. (2017a). The modeling displayed in Fig. 12 projects the real space three-dimensional correlation function into photometric space assuming Gaussian photometric redshift errors per galaxy, provided in Table 2 as σ_{68} . It also assumes a linear bias betweeen the galaxies and the matter field.

The bias recovered from the three-dimensional projected clustering at a mean redshift of 0.8 is $b = 1.83 \pm 0.06$, consistent with the one from $w(\theta)$ tomography. In addition we stress that this clustering estimate includes all cross-correlations of the data. The fact that it is matched by the theory modeling, which in turn includes a characterisation of the redshift distributions per galaxy, represents also an additional consistency check of reliability of the photometric redshifts.

8 CONCLUSIONS

This paper describes the selection of a sample of galaxies, optimised for BAO distance measurements, from the first year of DES data. By construction, this sample is dominated by red and luminous galaxies with redshifts in the range 0.6 < z < 1.0. We have extended the selection of red galaxies beyond that of previously published imaging data used for similar goals in SDSS by Padmanabhan et al. (2005) to cover the higher redshift and deeper data provided by DES.

We compute the expected magnitudes of galaxy templates in the four DES filters and identify the (i - z) and (z - i) color space to select red galaxies in the redshift range of interest. The actual selection in color and magnitude is defined using the BAO distance measurement figure-of-merit as a guiding criteria. Remark-

³ We make this choice throughout the DES-Y1 BAO analysis because the MICE N-Body simulation was used to calibrate the Halogen mock galaxy catalogues. MICE cosmology assumes a flat concordance LCDM model with $\Omega_{\text{matter}} = 0.25$, $\Omega_{\text{baryon}} = 0.044$, $n_s = 0.95$, $\sigma_8 = 0.8$ and h = 0.7.

⁴ The best-fit bias and error from the theory covariance or the mocks one are consistent with each other, however the χ^2 values are only so to about 40%.

ably, the resulting forecast matches the results obtained in DES-BAO-MAIN with the final analysis. The global flux limit of the sample is $i_{\rm auto} < 22$, although we later introduce a sliding magnitude cut to limit ourselves to brighter objects towards lower redshifts.

We consider three different photo-*z* catalogues, with two different photometric determinations. We showed that the typical photo-*z* uncertainty (in units of 1 + z) goes from 2.3% to 3.6% from low to high redshift, for DNF redshifts using MOF photometry, and slightly worse for BPZ with MOF photometry. Hence the former constitutes our primary catalogue in DES-BAO-MAIN, while the later is used for consistency. Redshift estimations based on COADD photometry turned out to be worse than those derived from MOF photometry by 10% - 20%. Our final sample is made of 1.3 million red galaxies across 1318 deg² of area, largely contained in one compact region (SPT).

We study and mitigate, when needed, observational systematics traced by various survey property maps. Of these, the most impactful is the stellar contamination, which we find nonetheless bound to < 4%. Also *i*-band mean seeing and *g*-band depth are relevant. We define weights to be applied to the galaxies when computing pair counting to remove the relations between galaxy number density and large scale fluctuations in those survey properties. We show that none of these corrections have an impact on BAO measurements, mainly because they can eventually modify the broad-shape of the correlation functions but do not introduce a characteristic localised scale as the BAO.

Lastly we characterised the two-point clustering of the sample, which is then used in DES-BAO-MAIN to derived distance constraints. We find the auto-correlations to be consistent with a bias that evolves only slightly with redshift, from 1.8 to 2. The bias derived from the tomographic analysis is consistent with the one fitted to the whole sample range with the 3D projected distance analysis. Furthermore we investigate the cross-correlation between all the tomographic bins finding clustering amplitudes matching expectactions, although with poor χ^2 -values in some cases. Overall this is a further test of the assumed redshift distributions.

This paper serves the purpose of enabling for the fist time BAO distance measurements using photometric data to redshifts $z \sim 1$. These measurements achieve a precision comparable to those considered state-of-the-art using photometric redshift to this point (Seo et al. 2012), as well as those from WiggleZ (Blake et al. 2011), which are both limited to $z \sim 0.65$. These BAO results are presetend in detail in DES-BAO-MAIN. While this paper was completed, the third year of DES data was made available to the collaboration, totalling 3 to 4 times the area presented here, and similar or better depth. Hence we look forward to that analysis, which should already yield a very interesting counter-part to the high precision low-z BAO measurements already existing.

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